

Student (Print) _____ Section _____

Last, First Middle

Student (Sign) _____

Student ID _____

Instructor _____

MATH 152
Exam1
Fall 2000
Test Form A

1-10	/50
11	/10
12	/10
13	/10
14	/10
15	/10
TOTAL	

Part I is multiple choice. There is no partial credit.

Part II is work out. Show all your work. Partial credit will be given.

You may not use a calculator.

Formulas:

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$\sin A \sin B = \frac{1}{2} \cos(A - B) - \frac{1}{2} \cos(A + B)$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\sin A \cos B = \frac{1}{2} \sin(A - B) + \frac{1}{2} \sin(A + B)$$

$$\cos A \cos B = \frac{1}{2} \cos(A - B) + \frac{1}{2} \cos(A + B)$$

$$\sin^2 A = \frac{1 - \cos 2A}{2}$$

$$\int \sec \theta d\theta = \ln|\sec \theta + \tan \theta| + C$$

$$\cos^2 A = \frac{1 + \cos 2A}{2}$$

$$\int \csc \theta d\theta = \ln|\csc \theta - \cot \theta| + C$$

$$\int \ln x dx = x \ln x - x + C$$

Part I: Multiple Choice (5 points each)

There is no partial credit. You may not use a calculator.

1. What is the average value of the function $f(x) = x^3$ on the interval $[-1, 2]$.

- a. $\frac{5}{4}$
- b. $\frac{15}{4}$
- c. 4
- d. $\frac{4}{3}$
- e. $\frac{20}{3}$

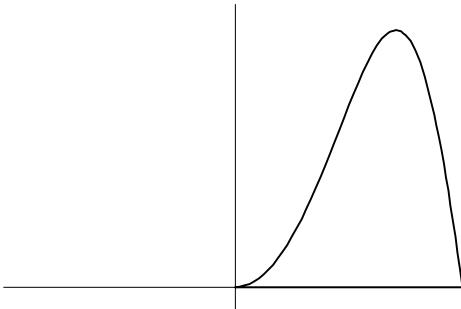
2. Using a trigonometric substitution, the integral $\int \frac{dx}{\sqrt{9+x^2}}$ becomes:

- a. $\int \sec \theta d\theta$
- b. $\int \frac{d\theta}{3 \sec \theta}$
- c. $\int \frac{d\theta}{\sec \theta}$
- d. $\int 3 \tan \theta d\theta$
- e. $\int \frac{d\theta}{\tan \theta}$

3. The region bounded by the curves

$$y = \sin(x^2), \quad y = 0, \quad x = 0 \quad \text{and} \quad x = \sqrt{\pi}$$

is rotated about the y -axis. Find the volume.



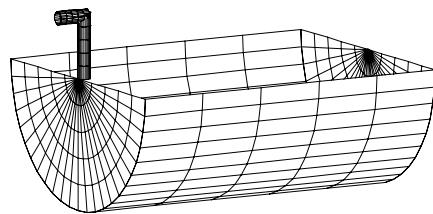
- a. 1
- b. 2
- c. π
- d. 2π
- e. 4π

4. A tank has the shape of a half cylinder which is 5 m long and 2 m in radius laying on its side. The tank is full of water. Which integral gives the work done to pump the water out of a spout which is 1 m above the tank.

The density of water is $\rho = 1000 \text{ kg/m}^3$.

The acceleration of gravity is $g = 9.8 \text{ m/sec}^2$.

Measure y down from the axis of the cylinder.



a. $9800 \int_{-2}^2 (y+1)10\sqrt{4-y^2} dy$

b. $9800 \int_{-2}^2 (1-y)5\sqrt{4-y^2} dy$

c. $9800 \int_0^2 (1-y)10(2-y) dy$

d. $9800 \int_0^2 (y+1)5(2-y) dy$

e. $9800 \int_0^2 (y+1)10\sqrt{4-y^2} dy$

5. Compute $\int_0^1 (x-2) e^x dx$.

a. $1 - 2e$

b. 1

c. $3 - 2e$

d. $-2e$

e. 3

6. Evaluate $\int \cos^3 x dx$.

- a. $\frac{\sin^4 x}{4} + C$
- b. $\frac{\sin^2 x}{2} - \frac{\sin^4 x}{4} + C$
- c. $\frac{\cos^4 x}{4} + C$
- d. $\sin x - \frac{\sin^3 x}{3} + C$
- e. $-\frac{\cos^4 x}{4} + C$

7. Which of these integrals represents the area between the curves $y = \sin x$ and $y = \cos x$ from $x = 0$ to $x = \pi$.

- a. $\int_0^{\pi/4} (\cos x - \sin x) dx + \int_{\pi/4}^{3\pi/4} (\sin x - \cos x) dx + \int_{3\pi/4}^{\pi} (\cos x - \sin x) dx$
- b. $\int_0^{\pi/4} (\cos x - \sin x) dx + \int_{\pi/4}^{\pi} (\sin x - \cos x) dx$
- c. $\int_0^{\pi/4} (\sin x - \cos x) dx + \int_{\pi/4}^{\pi} (\cos x - \sin x) dx$
- d. $\int_0^{\pi} (\cos x - \sin x) dx$
- e. $\int_0^{\pi} (\sin x - \cos x) dx$

8. Evaluate $\int_0^4 x \sqrt{9 + x^2} dx$.

- a. $\frac{147}{2}$
- b. $\frac{98}{3}$
- c. 6
- d. $\frac{392}{3}$
- e. $\frac{8}{3}$

9. The base of a solid is the circle $x^2 + y^2 = 9$. The cross sections perpendicular to the x -axis are squares. Find the volume.
- a. 9π
 - b. 36
 - c. 72
 - d. 81π
 - e. 144
10. What is the form of the partial fraction decomposition of $\frac{x^2 + 3}{x^3 - 2x^2 + x}$?
- a. $\frac{A}{x} + \frac{B}{x^2} + \frac{C}{(x - 1)^2}$
 - b. $\frac{A}{x^3} + \frac{B}{2x^2} + \frac{C}{x}$
 - c. $\frac{A}{x} + \frac{B}{x - 1} + \frac{C}{(x - 1)^2}$
 - d. $\frac{A}{x} + \frac{B}{(x - 1)^2}$
 - e. $\frac{A}{x} + \frac{B}{x^2} + \frac{C}{x - 1} + \frac{D}{(x - 1)^2}$

Part II: Work Out (10 points each)

Show all your work. Partial credit will be given.

You may not use a calculator.

11. Compute $\int x^3 \ln x dx$.

12. Find the area between the curves $x = y^2 - 1$ and $y = x - 5$.

a. (4 pts) Graph the curves.

b. (4 pts) Set up the integral(s) for the area.

c. (2 pts) Compute the area.

13. Compute $\int_0^{\pi/3} \tan^3 x \sec x dx.$

14. Evaluate $\int_0^{\sqrt{2}/2} \frac{x^2}{\sqrt{1-x^2}} dx.$

15. Consider the region in the plane bounded by the curves $\sqrt{x-1}$, $x = 3$, $x = 6$ and $y = 0$.

a. (3 pts) Graph the region.

b. (1 pt) The region is rotated about the x -axis. To find the volume, you will use

an x -integral

a y -integral

(Circle one.)

with

disks

washers

cylindrical shells

(Circle one.)

c. (4 pts) Set up the integral(s) for the volume.

d. (2 pts) Compute the volume.