

Name _____ ID _____

MATH 171

Exam 3

Spring 2004

Sections 502

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On the front of the Blue Book, on the Scantron and on this sheet

write your Name, your University ID and "Exam 3."

On the front of the Blue Book copy the Grading Grid shown at the right.

Enter your Multiple Choice answers on the Scantron

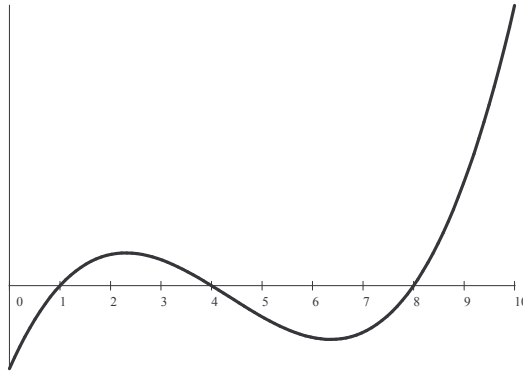
and CIRCLE them on this sheet.

1-10	/60
11	/15
12	/10
13	/15
Total	/100

Multiple Choice: (6 points each. No part credit.)

- Find the absolute minimum and absolute maximum values of the function $f(x) = x^3 - \frac{9}{2}x^2 + 14$ on the interval $[-2, 4]$.
 - minimum = -12 , maximum = 6
 - minimum = -12 , maximum = 14
 - minimum = -12 , maximum = $\frac{1}{2}$
 - minimum = $\frac{1}{2}$, maximum = 14
 - minimum = $\frac{1}{2}$, maximum = 6
- Where is $f(x) = \frac{1}{4}x^4 - 6x^2$ concave up?
 - $x < -2$ or $x > 2$
 - $-2 < x < 2$
 - $x < -\sqrt{12}$ or $0 < x < \sqrt{12}$
 - $-\sqrt{12} < x < 0$ or $x > \sqrt{12}$
 - $-\sqrt{12} < x < \sqrt{12}$

3. At the right is the graph of $y = f'(x)$.
Where is $f(x)$ increasing?



- a. $[0, 2.5]$ and $[6.5, 10]$
- b. $[0, 1]$ and $[4, 8]$
- c. $[2.5, 6.5]$
- d. $[1, 4]$ and $[8, 10]$
- e. $[4.5, 10]$
4. The graph of $y = f'(x)$ appears in the previous problem. Where does $f(x)$ have a local maximum?
- a. 1 and 8 only
- b. 2.5 only
- c. 4 only
- d. 1, 4 and 8 only
- e. 2.5 and 10 only
5. Find all critical points of the function $f(x) = \sin x + \cos x$ on the interval $[0, 2\pi]$.
- a. $\frac{\pi}{4}$ and $\frac{5\pi}{4}$ only
- b. $\frac{\pi}{4}$ only
- c. $\frac{5\pi}{4}$ only
- d. $\frac{3\pi}{4}$ and $\frac{7\pi}{4}$ only
- e. $\frac{3\pi}{4}$ only

6. A rocket starts at rest at ground level. Its vertical acceleration is $a(t) = 64\pi \sin(2t) - 32$ ft/sec² where t is in sec. What is its velocity at $t = \frac{\pi}{2}$ sec?
- a. 16π
 - b. 32π
 - c. 48π
 - d. 64π
 - e. 72π
7. Compute $\int_0^1 e^x dx$.
- a. e^2
 - b. $\frac{e^2}{2}$
 - c. $\frac{e^2}{2} - e$
 - d. e
 - e. $e - 1$
8. Find the area under $y = x^3$ between $x = 0$ and $x = 4$.
- a. 8
 - b. 16
 - c. 32
 - d. 64
 - e. 128
9. Compute $\int_0^1 x^2 \sin(4x^3) dx$.
- a. $12 - 12 \cos 4$
 - b. $12 \cos 1 - 12$
 - c. $\frac{1}{12} - \frac{1}{12} \cos 4$
 - d. $\frac{1}{12} \cos 4 - \frac{1}{12}$
 - e. $\frac{1}{12} \cos 1 - \frac{1}{12}$

10. Compute $\int_1^e \frac{(\ln x)^2}{x} dx$.

a. $\frac{1}{3}$

b. 2

c. $\frac{e^3 - 1}{3}$

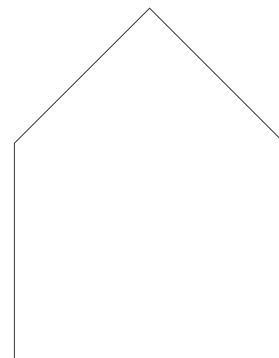
d. $2e - 2$

e. $\frac{2e - 2}{3}$

Work Out: (Points indicated. Part credit possible.)

Start each problem on a new page of the Blue Book. Number the problem. Show all work.

11. (15 points) A church window will have the shape of a rectangle with an isosceles right triangle on top. The area of the window is to be $A = 1 + 2\sqrt{2}$. Since the window frame will be gold plated, we want to minimize the perimeter of the window. What are the dimensions of the rectangular part of the window which minimize the perimeter of the whole window?



You must explain your solution using sentences.

HINT: If a is the height of the rectangle and b is its width, then $\frac{b}{\sqrt{2}}$ is the length of each slanted side of the triangular top.

12. (10 points) Let P_n denote the statement: $\sum_{i=1}^n 3^i = \frac{3^{n+1} - 3}{2}$

Use mathematical induction to prove P_n is true for all integers $n \geq 1$.

13. (15 points) Use the Method of Riemann Sums with Right Endpoints

to compute the integral $\int_1^4 (x - 1)^2 dx$. Use the F.T.C. only to check your answer.

Hints: $\sum_{i=1}^n 1 = n$ $\sum_{i=1}^n i = \frac{n(n+1)}{2}$ $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$