Name_____ Sec_____

1-12	/60	15	/11
13	/11	16	/12
14	/11	Total	/105

MATH 251 Exam 1 Spring 2011

Section 500 P. Yasskin

Multiple Choice: (5 points each. No part credit.)

1. Consider the line $X = P + t\vec{v}$ where $P = (2,3,2)$ and $\vec{v} = (2,-1,2)$.
Drop a perpendicular from the point $Q = (-1,0,5)$ to a point R on the line. Then $R =$
HINT: Draw a figure.

a. $\left(\frac{2}{3}, \frac{1}{3}, \frac{2}{3}\right)$

b. $\left(\frac{8}{3}, \frac{8}{3}, \frac{8}{3}\right)$

c. $\left(\frac{2}{3}, -\frac{1}{3}, \frac{2}{3}\right)$

d. $(4,2,4)$

e. $\left(\frac{8}{3}, \frac{10}{3}, \frac{8}{3}\right)$

2. If $\vec{u}$ is 5 cm long and points $30°$ WEST of NORTH and $\vec{v}$ is 4 cm long and points $30°$ EAST of NORTH, then $\vec{u} \times \vec{v}$ is

a. 10 cm long and points DOWN.
b. 10 cm long and points UP.
c. 10 cm long and points SOUTH.
d. $10\sqrt{3}$ cm long and points DOWN.
e. $10\sqrt{3}$ cm long and points SOUTH.

3. Find the point where the line $(x,y,z) = (3-2t, 2-t, 1+t)$ intersects the plane $x + y + 3z = 2$.
At this point, $x + y + z =$

a. 2
b. 4
c. 6
d. 8
e. The line does not intersect the plane.

4. The graph of the equation $x^2 + 4x - y^2 + 4y + z^2 + 2z = -1$ is a

a. hyperboloid of one sheet
b. hyperboloid of two sheets
c. cone
d. hyperbolic paraboloid
e. hyperbolic cylinder

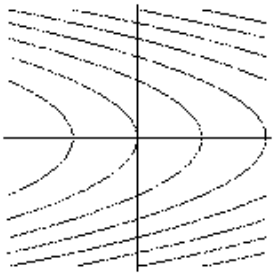
5. For the helix $\vec{r}(t) = (3t, \sin(4t), \cos(4t))$, which of the following is FALSE?

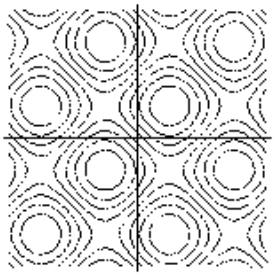
a. $\vec{v} = (3, 4\cos(4t), -4\sin(4t))$
b. $\vec{a} = (0, -16\sin(4t), -16\cos(4t))$
c. $\vec{j} = (0, -64\cos(4t), 64\sin(4t))$
d. speed $= 25$
e. arclength between $(0,0,1)$ and $(3\pi, 0, 1)$ is 5π

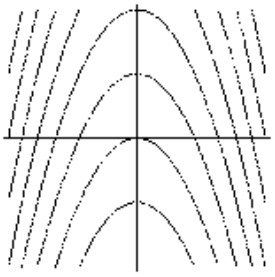
6. For the helix $\vec{r}(t) = (3t, \sin(4t), \cos(4t))$, which of the following is FALSE?

a. $\hat{T} = \left(\frac{3}{5}, \frac{4}{5}\cos(4t), -\frac{4}{5}\sin(4t)\right)$
b. $\hat{N} = (0, -\sin(4t), -\cos(4t))$
c. $\hat{B} = \left(-\frac{4}{5}, -\frac{3}{5}\cos(4t), -\frac{3}{5}\sin(4t)\right)$
d. $a_T = 0$
e. $a_N = 16$

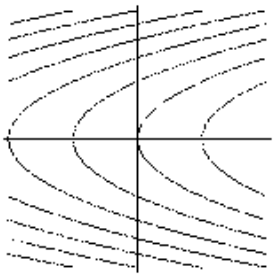
7. Which of the following is the contour plot of $f(x,y) = y^2 + x + 1$?

a. 

b. 

c. 

d. 

e. 

8. If $P(2,3) = 5$ and $\frac{\partial P}{\partial x}(2,3) = 0.4$ and $\frac{\partial P}{\partial y}(2,3) = -0.3$, estimate $P(2.1, 2.8)$.

a. 4.9
b. 4.98
c. 4.99
d. 5.01
e. 5.1

9. Currently for a certain box, the length L is 5 cm and increasing at 0.2 cm/sec, the width W is 4 cm and decreasing at 0.3 cm/sec, the height H is 3 cm and increasing at 0.1 cm/sec. Then currently, the volume V is

a. increasing at 0.1 cm/sec.
b. decreasing at 0.1 cm/sec.
c. increasing at 0.2 cm/sec.
d. decreasing at 0.2 cm/sec.
e. increasing at 0.3 cm/sec.

10. The temperature of a frying pan is $T = \frac{1}{1+x^2+4y^2}$. An ant is located at $(2,1)$. In what **unit vector** direction should the ant move to **decrease** the temperature as fast as possible?

a. $(-1,-2)$

b. $(1,2)$

c. $(1,-2)$

d. $\left(\frac{-1}{\sqrt{5}}, \frac{-2}{\sqrt{5}}\right)$

e. $\left(\frac{1}{\sqrt{5}}, \frac{2}{\sqrt{5}}\right)$

11. The temperature of a frying pan is $T = \frac{1}{1+x^2+4y^2}$. An ant is located at $(2,1)$ and has velocity $\vec{v} = (0.3,-0.6)$. What is the rate of change of the temperature as seen by the ant?

a. $-.0444$

b. -0.2

c. 0.2

d. 0.3333

e. 0.0444

12. The point $(2,1,-1)$ is on the graph of $x^2yz^2 + xy^3z = 2$. Compute $\left.\frac{\partial z}{\partial y}\right|_{(2,1)}$.

a. $-\frac{2}{3}$

b. $-\frac{1}{3}$

c. $\frac{1}{3}$

d. $\frac{2}{3}$

e. $\frac{4}{3}$

Work Out: (Points indicated. Part credit possible. Show all work.)

13. (11 points) Find the mass of the helical wire $\vec{r}(t) = (3t, \sin(4t), \cos(4t))$ from $(0,0,1)$ to $(3\pi,0,1)$ if its linear density is $\rho = x^2 + y^2 + z^2$.

14. (11 points) A bead slides along the helix $\vec{r}(t) = (3t, \sin(4t), \cos(4t))$ from $(0,0,1)$ to $(3\pi,0,1)$ under the action of the force $\vec{F} = (x, xy, xz)$. Find the work done.

15. (11 points) Find the plane tangent to the graph of the function $z = x^2y + y^3x$ at the point $(x,y) = (2,1)$. Find the z-intercept.

16. (12 points) Find the plane tangent to the level surface $x\sin z + y\cos z = 3$ at the point $(x,y,z) = \left(3,2,\frac{\pi}{2}\right)$. Find the z-intercept.