

MATH 253 Spring 2003 Section 501

Maple Quiz Solutions

```
> restart:with(VecCalc):VCalias:
```

```
#1
```

```
> f:=MF(<x,y>,x^2*y^4);
```

$$f := (x, y) \rightarrow x^2 y^4$$

```
> fx:=D[1](f);
```

$$fx := (x, y) \rightarrow 2 x y^4$$

```
> fy:=D[2](f);
```

$$fy := (x, y) \rightarrow 4 x^2 y^3$$

```
> P:=<2,1>;
```

$$P := \begin{bmatrix} 2 \\ 1 \end{bmatrix}$$

```
> X:=<x,y>;
```

$$X := \begin{bmatrix} x \\ y \end{bmatrix}$$

```
> fP:=f &@ P;
```

$$fP := 4$$

```
> fxP:=fx &@ P;
```

$$fxP := 4$$

```
> fyP:=fy &@ P;
```

$$fyP := 16$$

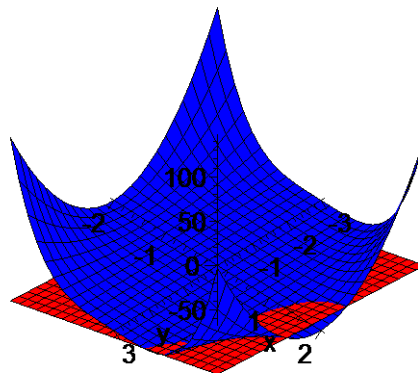
```
> ftan:=MF(<x,y>,fP+fxP*(x-2)+fyP*(y-1));
```

$$ftan := (x, y) \rightarrow -20 + 4 x + 16 y$$

```
> pf:=plot3d(f(x,y), x=-3..3, y=-2..2, color=blue):
```

```
> pftan:=plot3d(ftan(x,y), x=-3..3, y=-2..2, color=red):
```

```
> display(pf,pftan, axes=normal);
```



```

[ #2
[ > z0:=rho*cos(phi);
                                z0 := ρ cos(ϕ)
[ > J:=rho^2*sin(phi);
                                J := ρ2 sin(ϕ)
[ > M:=Muint(z0*J, rho=0..2, theta=0..2*Pi, phi=0..Pi/2); M:=value(%);
                                M := ∫0π ∫02π ∫02 ρ3 cos(ϕ) sin(ϕ) dρ dθ dϕ
                                M := 4 π
[ > Mz:=Muint(z0^2*J, rho=0..2, theta=0..2*Pi, phi=0..Pi/2);
Mz:=value(%);
                                Mz := ∫0π ∫02π ∫02 ρ4 cos(ϕ)2 sin(ϕ) dρ dθ dϕ
                                Mz :=  $\frac{64 \pi}{15}$ 
[ > zbar:=Mz/M;
                                zbar :=  $\frac{16}{15}$ 
[ >

```