

Name \_\_\_\_\_ ID \_\_\_\_\_

1-4	/40	7	/15
5	/15	8	/15
6	/15	E.C.	/10

MATH 311                      Exam 3                      Fall 2002  
 Section 200                      P. Yasskin

Multiple Choice: (10 points each)      Work Out: (15 points each)      Extra Credit: (10 points)

- If  $\vec{V} \times \vec{F} = (2x^2y - x^2, y^2 - 2xy^2, 2xz - 2yz)$ , then  $\vec{V} \cdot (\vec{V} \times \vec{F}) =$

  - $(4xy - 2x, 4xy - 2y, 2x - 2y)$
  - $(4xy - 2x, 2y - 4xy, 2x - 2y)$
  - $8xy - 4y$
  - 0
  - $2x^2 - 2y^2$
  
- If  $\vec{V} \times \vec{F} = (2x^2y - x^2, y^2 - 2xy^2, 2xz - 2yz)$ , then  $\vec{V} \times (\vec{V} \times \vec{F}) =$

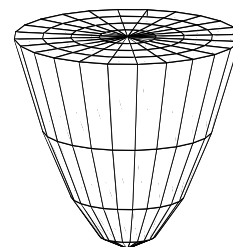
  - $(4xy - 2x, 4xy - 2y, 2x - 2y)$
  - $(4xy - 2x, 2y - 4xy, 2x - 2y)$
  - $(-2z, -2z, -2x^2 - 2y^2)$
  - $(-2z, 2z, -2x^2 - 2y^2)$
  - $-2x^2 - 2y^2$
  
- If  $\vec{G} = (2x^2y - x^2, y^2 - 2xy^2, 2xz - 2yz)$ , then  $\vec{G} = \vec{\nabla}g$  where  $g(0, 1, 1) - g(0, 1, 0) =$

  - 2
  - 1
  - 0
  - 1
  - The scalar potential  $g$  does not exist.
  
- Compute  $\oint (y+z) dx + (x+z) dy + (x+y) dz$  clockwise around the circle  $x^2 + y^2 = 9$  with  $z = 5$ .  
 HINT: Use a theorem.

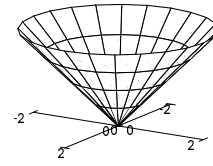
  - $-18\pi$
  - $-9\pi$
  - 0
  - $9\pi$
  - $18\pi$

5. Compute  $\oint_{\partial T} (xy) dx + (xy) dy$  counterclockwise around the boundary of the triangle with vertices  $(0,0)$ ,  $(1,0)$  and  $(0,2)$ .

6. Compute  $\iint_{\partial P} \vec{E} \cdot d\vec{S}$  for  $\vec{E} = (xz, yz, z^2)$  over the **complete** surface of the solid paraboloid  $P$  given by  $x^2 + y^2 \leq z \leq 4$  with outward normal.



7. The cone  $z = \sqrt{x^2 + y^2}$  for  $z \leq 2$  is shown at the right. Find the mass and center of mass of the cone if its surface density is given by  $\delta = x^2 + y^2$ .



8. Compute  $\iint_S \vec{\nabla} \times \vec{F} \cdot d\vec{S}$  for  $\vec{F} = (x^2y, -x^3, z^2)$

over the piece of the sphere  $x^2 + y^2 + z^2 = 25$

for  $0 \leq z \leq 4$  with normal pointing away from the  $z$ -axis.

Hint: Parametrize the upper and lower edges.



**Extra Credit** Redo #8 but compute  $\iint_S \vec{\nabla} \times \vec{F} \cdot d\vec{S}$  directly as a surface integral.