

Group Member Names:

```
In [1]: from sympy import *
        from sympy.plotting import plot, plot_parametric
```

## Lab 5 Template

Each part of each problem should be solved in its own cell.

### Question 1

Let  $x(t) = t \cos(t)$  and  $y(t) = t \sin(t)$ .

a.) Plot the curve in three **separate** plots using  $t = [-\pi/4, \pi/4]$ ,  $t = [-\pi, \pi]$ , and  $t = [-3\pi/2, 3\pi/2]$  using **ylim=[-5, 2]** and **xlim=[-5, 5]**.

b.) Find the approximate points on the graph (using **nsolve** and giving  $(x, y)$  pairs **not**  $t$  values) such that the tangent line is horizontal. (Hint: you need to give **nsolve** a guess to work properly. For this part, you'll need to use **nsolve** with 3 different guesses that yield three separate  $t$  values. It may take a few tries to get it right)

c.) Find the approximate points on the graph (using **nsolve**) such that the tangent line is vertical.

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### Question 2

Let  $x(t) = 2 \cos(t) + \cos(2t)$  and  $y(t) = 2 \sin(t) - \sin(2t)$ .

a.) Plot the curve for  $t = [0, 6]$ .

b.) Find the equation for the tangent line at  $(-1, 2)$ . (You may need to use **nsolve** for this part and use the plot to pick a good guess)

c.) Find all points where the curve has a vertical tangent line for  $t$  in the interval  $[0, 6]$ . (Hint: Be careful which  $t$  values you use when finding the point and make sure to verify that your  $t$  value makes sense. Many  $t$  values may look like possible answers, but they are not.)

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### Question 3

Find  $\frac{dy}{dx}$  for the following functions and be sure to use **.simplify()** on your final answer.

a.)  $y = x^{\sin(x^2)}$

b.)  $y = \arctan(\arccos(e^x))$

c.)  $y^2 + \sin(y) = \frac{x^2-1}{x^3+7}$  (Hint: If you have  $f(y) = g(x)$ , then  $\frac{dy}{dx} = \frac{g'(x)}{f'(y)}$ ). Also for this problem, use **.factor()** instead of **.simplify()**

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