MATH151, Fall 2022 Common Exam I - Version A

LAST NAME (print):	FIRST NAME (print):
INSTRUCTOR:	
SECTION NUMBER:	-
DIRECTIONS:	
• No calculators, cell phones, smar must be put away.	et watches, headphones, or other electronic devices may be used, and
• TURN OFF cell phones and put be collected and you will receive	them away. If a cell phone is seen during the exam, your exam will a zero.
	ce on your ScanTron using a No. 2 pencil. The scantrons will not be a records, also record your choices on your exam!
	ns in the space provided. Show all your work neatly and concisely, nswer. You will be graded not merely on the final answer, but also f the work leading up to it.
• Be sure to fill in your name the ScanTron form.	e, UIN, section number, and version letter of the exam on
7	THE AGGIE HONOR CODE
"An Aggie does not	lie, cheat or steal, or tolerate those who do."
Signature:	

Part I: Multiple Choice. 3 points each

- 1. Find a vector of length 3 in the same direction as the vector from the point (-2,3) to (1,-1).
 - (a) $\left\langle \frac{9}{5}, -\frac{12}{5} \right\rangle$
 - (b) $\left\langle -\frac{9}{5}, \frac{12}{5} \right\rangle$
 - (c) $\left\langle \frac{9}{\sqrt{5}}, -\frac{12}{\sqrt{5}} \right\rangle$
 - (d) $\left\langle -\frac{3}{\sqrt{5}}, \frac{6}{\sqrt{5}} \right\rangle$
 - (e) $\left\langle -\frac{3}{\sqrt{17}}, -\frac{12}{\sqrt{17}} \right\rangle$

- 2. Find a vector equation of the line that passes through (-6,4) and is perpendicular to the line with parametric equations x = 7 + 2t, y = 1 3t.
 - (a) $\mathbf{r}(t) = \langle 4 + 3t, -6 + 2t \rangle$
 - (b) $\mathbf{r}(t) = \langle -6 t, 4 + 7t \rangle$
 - (c) $\mathbf{r}(t) = \langle -6 + 2t, 4 3t \rangle$
 - (d) $\mathbf{r}(t) = \langle 4 + 2t, -6 3t \rangle$
 - (e) $\mathbf{r}(t) = \langle -6 + 3t, 4 + 2t \rangle$

- 3. Find $\lim_{x \to \infty} \left[\ln(5x^2 + 1) \ln(x^3 + x 4) \right]$.
 - (a) ∞
 - (b) $-\infty$
 - (c) 0
 - (d) ln(5)
 - (e) $\frac{2}{3}$

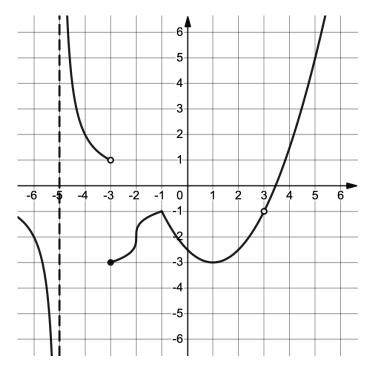
- 4. Find the cosine of the angle between the vectors $\langle -3, 5 \rangle$ and $\langle -2, 1 \rangle$.
 - (a) $\frac{11}{\sqrt{34}\sqrt{5}}$
 - (b) $\frac{11}{\sqrt{2}}$
 - (c) $\frac{11}{4\sqrt{5}}$
 - $(d) -\frac{1}{\sqrt{34}\sqrt{5}}$
 - (e) $\frac{30}{\sqrt{34}\sqrt{5}}$
- 5. Find the scalar projection of $\mathbf{b} = 3\mathbf{i} + 2\mathbf{j}$ onto $\mathbf{a} = 2\mathbf{i} 5\mathbf{j}$.
 - (a) $-\frac{4}{\sqrt{13}}$
 - (b) $\frac{2}{\sqrt{34}}$
 - (c) $-\frac{4}{\sqrt{29}}$
 - (d) $\frac{4}{\sqrt{29}}$
 - (e) $\frac{4}{\sqrt{13}}$
- 6. Find $\lim_{x \to -\infty} \frac{2x+3}{\sqrt{9x^2-2x+5}}$.
 - (a) $\frac{2}{3}$
 - (b) $-\frac{2}{9}$
 - (c) $\frac{2}{9}$
 - (d) $-\frac{2}{3}$
 - (e) 0

- 7. Which of the following is equal to $\tan\left(\arccos\left(\frac{x}{2}\right)\right)$?
 - (a) $\frac{\sqrt{4+x^2}}{x}$
 - (b) $\frac{\sqrt{4-x^2}}{x}$
 - (c) $\frac{\sqrt{4-x^2}}{2}$
 - (d) $\frac{x}{\sqrt{4-x^2}}$
 - (e) $\frac{2}{\sqrt{4-x^2}}$

- 8. Find $\lim_{x \to 2^-} \frac{3x+6}{x-2}$.
 - (a) ∞
 - (b) 0
 - (c) 3
 - (d) 12
 - (e) $-\infty$

- 9. The position (in meters) of a particle after t seconds is given by $f(t) = (t+1)^2 1$. Find the average velocity of the particle from t = 1 to t = 3.
 - (a) 8 m/s
 - (b) 4 m/s
 - (c) 6 m/s
 - (d) $\frac{26}{3}$ m/s
 - (e) 9 m/s

Use the following graph of f to answer questions 10 and 11.



- 10. Given the graph of f above, which of the following is **false**?
 - (a) $\lim_{x \to 5} f(x) = 5$.
 - (b) $\lim_{x \to 3} f(x) = -1$.
 - (c) f is continuous from the left at x = -3.
 - (d) $\lim_{x \to -5^+} f(x) = \infty$.
 - (e) f is continuous at x = -1.

- 11. Given the graph of f above, for which value of x is f(x) differentiable?
 - (a) x = -3
 - (b) x = 3
 - (c) x = -1
 - (d) x = 1
 - (e) x = -2

- 12. A crate is hauled 10 meters up a ramp under a constant force of 7 Newtons applied at an angle of 30° to the ramp. Find the work done.
 - (a) $35\sqrt{2} \text{ J}$
 - (b) 35 J
 - (c) 70 J
 - (d) $35\sqrt{3} \text{ J}$
 - (e) None of these.

- 13. Find the value of a that makes $f(x) = \begin{cases} ax^2 2x & \text{if } x \leq 2 \\ 3x + a & \text{if } x > 2 \end{cases}$ continuous everywhere.
 - (a) 2
 - (b) $\frac{10}{3}$ (c) $\frac{2}{3}$

 - (d) 4
 - (e) There is no such a value.

- 14. According to the Intermediate Value Theorem, which of the following intervals contains a solution to the equation $x^3 - 4x - 5 = 0$?
 - (a) (-2, -1)
 - (b) (0,1)
 - (c) (-1,0)
 - (d) (2,3)
 - (e) (1,2)

- 15. Find $\lim_{x \to \infty} \frac{4x \sqrt{x^2 + 5x}}{3x}$.
 - (a) $\frac{4}{3}$
 - (b) $\frac{5}{3}$
 - (c) 1
 - (d) ∞
 - (e) $-\infty$

- 16. Find $\lim_{x \to -\infty} \frac{5e^{-2x} + 3e^{4x}}{2e^{-2x} e^{4x}}$.
 - (a) -3
 - (b) 0
 - (c) ∞
 - (d) $\frac{5}{2}$
 - (e) $-\infty$

- 17. Which of the following correctly describes the curve given by $\mathbf{r}(t) = \langle 1 + \sin t, -2 + \cos t \rangle$ as t increases?
 - (a) Clockwise around a circle with center (1, -2).
 - (b) Counterclockwise around a circle with center (1, -2).
 - (c) Clockwise around a circle with center (-1,2).
 - (d) Counterclockwise around a circle with center (-1, 2).
 - (e) None of these.

- 18. Find the horizontal and vertical asymptotes of $f(x) = \frac{x^2 4}{(2 x)(x + 3)}$.
 - (a) y = -1, x = 2, x = -3
 - (b) y = 1, x = -3
 - (c) y = -1, x = -3
 - (d) y = 1, x = 2
 - (e) y = -1, y = 1, x = -3

- 19. Find $\lim_{x \to \infty} \arctan\left(\frac{x x^3}{x + 7}\right)$.
 - (a) $\frac{\pi}{2}$
 - (b) $-\frac{\pi}{4}$
 - (c) $\frac{\pi}{4}$
 - (d) $-\infty$
 - (e) $-\frac{\pi}{2}$

- 20. Given $f(x) = x^3 4x + 1$ and $f'(x) = 3x^2 4$, find the equation of the tangent line to f(x) at x = -2.
 - (a) y = 8x 10
 - (b) y = 8x + 1
 - (c) y = x + 10
 - (d) y = 8x + 17
 - (e) y = x + 3

Part II: Work Out Problems

<u>Directions</u>: Present your solutions in the space provided. Show all your work neatly and concisely and box your final answer. You will be graded not merely on the final answer, but also on the quality and correctness of the work leading up to it.

- 21. (10 points) Two forces \mathbf{F}_1 and \mathbf{F}_2 act on an object. The force \mathbf{F}_1 has a magnitude of 26 lbs and a direction of 45° counterclockwise from the positive x-axis, and \mathbf{F}_2 has a magnitude of 8 lbs and a direction of 150° counterclockwise from the positive x-axis.
 - (a) Find the resultant force \mathbf{F} .

(b) Find the resultant angle θ as measured counterclockwise from the positive x-axis. Leave your answer in terms of an inverse trigonometric expression.

22. (15 points) Find the following limits. Do not use L'Hospital's Rule.

(a)
$$\lim_{x \to 6} \frac{(x-2)^2 - 16}{x^2 - 6x}$$

(b)
$$\lim_{x \to 2} \frac{\sqrt{5x+6}-4}{x-2}$$

(c)
$$\lim_{x \to -1^-} \frac{|x+1|}{x^2 + 3x + 2}$$

- 23. (6 points) Consider the function $f(x) = \begin{cases} 2e^{x+3} & \text{if } x \le -3\\ 3x-1 & \text{if } -3 < x < 1\\ \sqrt{x^2+3} & \text{if } x > 1 \end{cases}$
 - (a) Find $\lim_{x\to -3} f(x)$, or explain why it does not exist.

(b) Find $\lim_{x\to 1^+} f(x)$, or explain why it does not exist.

24. (9 points) Use the **definition** of the derivative to find f'(x) for $f(x) = \frac{4}{x-2}$. No points will be given for any shortcut formulas used!

Do not write in this table.

Question	Points Awarded	Points
1-20		60
21		10
22		15
23		6
24		9
Total		100