Invariant complementation and a separation property for a locally compact group

Let G be a locally compact group and VN(G) denote the von Neumann algebra generated by the left regular representation of G. In this talk, I shall describe an invariant complementation property for an invariant W^* -subalgebra of VN(G) and its relation with a separation for closed subgroups of G by continuous positive definite functions.