## Calculus

Instructions Please write your name in the upper right-hand corner of the page. Write complete sentences to explain your solutions.

1. Write down a function $f(x)$ whose graph looks like the picture. The key features of the picture are that $\lim _{x \rightarrow 1^{+}} f(x)=\infty, \lim _{x \rightarrow 1^{-}} f(x)=-\infty$, $\lim _{x \rightarrow \infty} f(x)=2$, and $\lim _{x \rightarrow-\infty} f(x)=2$. Explain the reasoning for your choice of $f(x)$.


## Calculus

2. The TI-89 calculator says that $\lim _{x \rightarrow 1}\left(\frac{1}{x-1}-\frac{2}{x^{2}-1}\right)=\frac{1}{2}$. Supply a computation that confirms this value. (Suggestion: combine the fractions with a common denominator and simplify.)
3. Find a number $c$ such that $\lim _{x \rightarrow \infty}\left(\sqrt{x^{2}+c x}-x\right)=3$.
