## Applied Algebra

Instructions Please write your name in the upper right-hand corner of the page. Use complete sentences, along with any necessary supporting calculations, to answer the following questions.

1. Consider the set of $2 \times 2$ matrices that have integer entries and determinant equal to 1 . Under the operation of matrix multiplication, does this set form a semigroup? a group? Explain.

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2. Here is a partially completed group table for a certain abelian group. Fill in the rest of the table. Notice that $a$, the first element, is not necessarily the identity element.

|  | $a$ | $b$ | $c$ | $d$ |
| :---: | :---: | :---: | :---: | :---: |
| $a$ | $b$ |  |  |  |
| $b$ |  |  |  | $d$ |
| $c$ |  | $c$ |  |  |
| $d$ | $c$ |  | $a$ |  |

