Suppose (X_1, τ_1) and (X_2, τ_2) are first-countable topological spaces. Is the product space $X_1 \times X_2$, equipped with the product topology, first-countable too? Prove or give a counterexample, as appropriate.