

1.2-Dot Product

Definitions:

The *dot product* of the vectors \mathbf{a} and \mathbf{b} is given by

Dot Product computation formula

From the definition, it follows that the angle between two vectors is given by

\mathbf{a} and \mathbf{b} are *orthogonal* if and only if

Orthogonal complements

Scalar and Vector projections

Work

Examples:

Find $\mathbf{a} \cdot \mathbf{b}$ if $\mathbf{a} = \langle 3, 2 \rangle$ and $\mathbf{b} = \mathbf{i} - 4\mathbf{j}$

Find the angle between $\mathbf{a} = \langle 3, 1 \rangle$ and $\mathbf{b} = \langle -2, 4 \rangle$.

Find x such that $\mathbf{a} = \langle x, 1 \rangle \perp \mathbf{b} = \langle 4 + x, 3 \rangle$

If $\mathbf{a} = \mathbf{i} + 3\mathbf{j}$ and $\mathbf{b} = \langle 4, 1 \rangle$, find the scalar and vector projection of \mathbf{a} onto \mathbf{b}

A 5 kg block slides down a frictionless ramp 5 meters tall and 12 meters long (horizontally). Find the work done by gravity if the block slides the entire length of the ramp.

On Your Own: #5,9,10,13,19,23,27,31,33,35,37,43,47,53,55,57