

## 1 2.7: Tangents, Velocities, and Rates of Change

We are now ready to find a formal way of computing the slope of the line tangent to the curve. Re-view the animation from 2.1 posted on my webpage. What happens as the second  $x$  coordinate moves closer to the given tangent line point?

Each secant line above passes through the point  $(1,1)$ . If  $x$  is the  $x$ -coordinate of the second point, write an expression for the slope of the line between the two points.

Write and solve a limit problem which allows us to find the slope of the tangent line at  $x = 1$ .

**More General:** Draw any function, a tangent line, and a secant line. Label the  $x$ -coordinate of the tangent line point  $a$  and the  $x$ -coordinate of the second point  $x$ .

$m_{sec} =$

What should happen as the point  $(x, f(x))$  moves closer to the tangent-line point  $(a, f(a))$ ? Write a limit which explains this mathematically:

$m_{tan} =$

**Most General:** Draw any function, a tangent line, and a secant line again in the space below. Label the  $x$ -coordinate of the tangent line  $a$  and let  $h$  be the horizontal distance between the  $x$  values on the secant line. (View the animation posted under today's notes for a visual understanding of this.)

$$m_{sec} =$$

$$m_{tan} =$$

The **derivative** of a function at  $x = a$  is given by

**Examples:**

Use a limit definition to find the equation of the line tangent to the curve  $f(x) = \frac{8}{x+2}$  at the point where  $x = 0$ .

**On Your Own:** Find the equation of the line tangent to the curve  $f(x) = x^2 - 4x + 4$  at the point where  $x = 3$ .

$$y = 2x - 5$$

**Secant and Tangent Vectors-an Introduction**

Find a vector tangent to the curve  $\mathbf{r}(t) = \sqrt{t-1}\mathbf{i} + (t^2 + t - 2)\mathbf{j}$  at the point  $(1, 4)$ . Then find parametric equations of the line tangent to the curve at this point.