

1. $\lim_{h \rightarrow 0} \frac{\sin(5h)}{\tan(3h)}$

a. $3/5$

b. $5/3$

c. 0

d. 1

e. ∞

2. Find the derivative of $f(x) = \frac{1}{(\csc^2(x) - \sin(2x^2))^4}$

a. $\frac{1}{(-\csc^2 x - 4x(\cos(2x^2)))^5}$

b. $8 \frac{\csc^2(x) \cot^2(x) + 2x \cos(2x^2)}{(\csc^2(x) - \sin(2x^2))^5}$

c. $-4(\csc^2(x) - \sin(2x^2))^{-5}$

d. $\frac{-4 \csc(x) \cot(x) - \cos(2x^2)}{\csc^2(x) - \sin(2x^2)^5}$

e. $-\csc(x) \cot(x) - 4x \cos(2x^2)$

3. Find the derivative of $f(x) = (\sin^2(\cos(4x)))$

a. $8\cos(\cos(4x)) \cdot \sin(4x)$

b. $-8\sin(\cos(4x)) \cdot \cos(\cos(4x)) \cdot \sin(4x)$

c. $\cos(\cos(4x)) \cdot \sin(4x) \cdot 4$

- d. $2\sin(x)\cos(4x)$
- e. $2(\cos(\cos(4x))\sin(4x))$
4. Suppose that $h(x)=f(x)g(x)$. $F(x)=f(g(x))$ where $f(2)=3$, $g(2)=5$, $g'(2)=4$, $f'(2)=-2$, and $f'(5)=11$. Find $h'(2)$ and $F'(2)$.
- a. $h'(2)=15$, $F'(2)=44$
- b. $h'(2)=2$, $F'(2)=44$
- c. $h'(2)=2$, $F'(2)=15$
- d. $h'(2)=15$, $F'(2)=4$
- e. $H'(2)=15$, $F'(2)=15$
5. Find a tangent vector of unit length to the equation $r(t)=\langle t\cos(t)+3t, \sin(t)+3 \rangle$ at $t=0$
- a. $(1, 0)$
- b. $\left\langle \frac{4}{\sqrt{17}}, \frac{1}{\sqrt{17}} \right\rangle$
- c. $\left\langle \frac{3}{\sqrt{10}}, \frac{1}{\sqrt{10}} \right\rangle$
- d. $\left\langle \frac{4}{\sqrt{5}}, \frac{1}{\sqrt{5}} \right\rangle$
- e. $\langle 4, 1 \rangle$
6. Find $f^{(53)}(\sin(2x))$

- a. $2^{53} \cos(2x)$
- b. $2^{106} \cos(2x)$
- c. $2^2 \cos(2x)$
- d. $2^{53} \sin(2x)$
- e. $-2^{106} \cos(2x)$
7. A point is moving on the curve $xy = 12$ ($x > 0$). The x coordinate of the point is increasing at the rate of 4 units/min. At what rate is the y coordinate changing when $x = 4$?
- a. 1
- b. 4
- c. -3
- d. 3
- e. -4
8. Differentiate the function: $g(x) = e^{-5x} \cos(3x)$
- a. $-15e^{-5x} \cos(3x)$
- b. $e^{-5x}(-3 \sin(3x) - 5 \cos(3x))$
- c. $5 \sin(3x)$
- d. $15e^{-5x} \sin(3x)$
- e. $e^{-5x}(\sin(3x) - 5 \cos(3x))$
9. $\lim_{x \rightarrow -\infty} \frac{e^{\pi x} - e^{-\pi x}}{e^{\pi x} + e^{-3\pi x}}$
- a. 0
- b. 1
- c. e
- d. $-\infty$
- e. ∞

10. Suppose g is the inverse function of a differentiable function f . Let $G(x) = 1/g(x)$. If $f(3) = 2$, and $f'(3) = (1/9)$ find $G'(2)$.
- 6
 - 1
 - 1
 - 6
 - 12

11. Express the following as a single log:

$$\log_2 x + 5 \log_2(x + 1) + \frac{1}{2} \log_2(x - 1)$$

- $\log_2(x - 5(x + 1) - \sqrt{x - 1})$
- $\log_2(x * (x + 1)^5 * \sqrt{x - 1})$
- $\log_2(x * \frac{(x+1)}{5} \sqrt{x - 1})$
- $\log_2(x * 5(x + 1) * .5(x - 1))$
- $\log_2(x * 5(x + 1) * \sqrt{x - 1})$

12. Find the inverse function of $y = \frac{1+e^x}{1-e^x}$

- $y = e^x + 1$
- $y = \ln \frac{x-1}{x+1}$
- $y = \ln 2x - 4$
- $y = \ln \frac{x+1}{x-1}$
- $y = e^x - 1$

FREE RESPONSE PRACTICE

13. $x^3 + y^3 = 6xy$
- Find the first derivative at the point (3,3)

- b. Find the second derivative at the point (3,3)
14. The vector functions represent the position of a particle at time t .
$$\mathbf{R}(t) = \sqrt{t^2 + 5}\mathbf{i} + t\mathbf{j}$$
- a. Find the velocity at $t=2$
- b. Find the speed at $t=2$
- c. Find the acceleration at $t=2$
15. Find the points on the curve $x = \frac{3t}{1+t^3}$ and $y = \frac{3t^2}{1+t^3}$ where the tangent is horizontal or vertical. List the point and specify whether it has a horizontal or vertical tangent.
16. A paper cup has the shape of a cone with height 10 cm and radius 3 cm at the top. If water is poured into the cup at a rate of $2 \text{ cm}^3/\text{s}$, how fast is the water level rising when the water is 5 cm deep?

17. The angle of elevation of the sun is decreasing at a rate of 0.25 radians/hour. How fast is the shadow cast by a 400 ft tall building increasing when the angle of elevation of the sun is $(\pi/6)$?

18. $f(x) = \frac{1}{(1+2x)^4}$.

Find the linear and quadratic approximations to $f(x)$ near $a=1$.

19. $F(x) = \sqrt{x-2}$. $a=2$.

a. Show that $F(x)$ is one to one

b. Find $G'(a)$ where G is the inverse of $F(x)$ using $G'(x) = \frac{1}{F'(G(x))}$

c. Calculate $G(x)$ and state the domain and range of $G(x)$

d. Calculate $G'(a)$ from the formula in part c.