A set is a collection of objects.
The objects in a set are the elements or members of the set.
$\rightarrow$ Always enclose the elements of a set in curly brackets.
A set with the numbers $-1,1,0$ would be written as
where is read "is an element of"
Define $S=$

More notation:

- 0 is the symbol for the real number zero
- $\{0\}$ is a set with one element, the real number zero
- $\varnothing$ is a set with zero elements, the empty set. Alternative is $\}$.
- $\{\varnothing\}$ is a set with one element, the symbol for the empty set.

Two sets are equal $(=$ ) if they contain exactly the same elements (order doesn't matter).

They are not equal $(\neq)$ if they don't contain the same elements.

Set builder notation: Describe the set in terms of its properties,

Roster notation: List the elements of the set.

## Subset:

Set $B$ is a subset of set $A$ (written $B \subseteq A$ ) if every element in $B$ is in $A$.

## Proper Subset:

Set $B$ is a proper subset of set $A$ (written $B \subset A$ ) if $B \subseteq A$ and $A \neq B$.

## Universal set:

The set from which all the member of other sets will be drawn. Called $U$.

## Venn Diagram notation:

- A rectangle represents the universal set
- Circles are sets in the universal set.

Example: Show the relationship between $E$ and $F$ (defined above) in a Venn diagram.

Given a set $A$ and a universal set $U$, the elements that are in $U$ and are NOT in $A$ is called the complement of $A$ or $A^{c}$.

Example: From the last example, $E$ is the set of positive even integers less than 17 , what is $E^{c}$ in roster notation?

Those elements that belong to both $A$ and $B$ are in the intersection of $A$ and $B, A \cap B$.

Example: Let $U=\{x \mid x$ is a card in a standard deck of 52 playing cards $\}$ $R=\{x \mid x$ is a red card $\}$ and $Q=\{x \mid x$ is a queen $\}$

Find $R \cap Q$ in roster notation.
If two sets have no elements in common, that is $A \cap B=\varnothing$, then the sets are disjoint.

Example: If $K=\{x \mid x$ is a king $\}$, find $K \cap Q$ in roster notation.

Those elements that belong to $A$ or $B$ are in the union, $A \cup B$.

Note: this is the inclusive or, not the exclusive or

Example Let $U=\{x \mid x$ is a card in a standard deck of 52 playing cards $\}$ $H=\{x \mid x$ is a heart card $\} \quad Q=\{x \mid x$ is a queen $\}$

Find $H \cup Q$ in roster notation.

Example Let $U=\{x \mid x$ is a letter in the English alphabet $\}=\{\mathrm{a}, \mathrm{b}, \mathrm{c}, \ldots, \mathrm{z}\}$

$$
\begin{aligned}
& A=\{x \mid x \text { is a vowel }\}=\{\mathrm{a}, \mathrm{e}, \mathrm{i}, \mathrm{o}, \mathrm{u}\} \\
& B=\{x \mid x \text { is a letter in the word texas }\}=\{\mathrm{t}, \mathrm{e}, \mathrm{x}, \mathrm{a}, \mathrm{~s}\}
\end{aligned}
$$

Find the following sets in roster notation.
a) What is $A \cap B$ ?

b) What is $A^{c} \cap B$ ?

c) What is $A \cup B^{c}$ ?


