$\mathrm{T}_{\mathrm{E}} \mathrm{X}$ document $\# 3$

$$
M=\int_{E} \rho d V
$$

We can do the integrations over the three coordinates in any order we choose. Here we have chosen to do the the $z$ integral first (that is, put it on the inside), then $y$, then $x$.

$$
\begin{aligned}
M & =\int_{0}^{1}\left[\int_{0}^{1}\left[\int_{0}^{2}(1+2 y) d z\right] d y\right] d x \\
& =\int_{0}^{1} \int_{0}^{1}[(1+2 y) z]_{z=0}^{2} d y d x \\
& =\int_{0}^{1} \int_{0}^{1} 2(1+2 y) d y d x \\
& =2 \int_{0}^{1}\left[y+y^{2}\right]_{0}^{1} d x \\
& =2 \int_{0}^{1}(1+1) d x \\
& =4 \int_{0}^{1} d x \\
& =4 \mathrm{~kg}
\end{aligned}
$$

