

6.4 - The Definite Integral

$\lim_{n \rightarrow \infty} \sum_{k=1}^n f(c_k) \Delta x$ is the definite integral of $f(x)$ on $[a, b]$.

Notation:

Geometric interpretation:

Properties: (in addition to all the previous properties of integrals)

$$1. \int_a^a f(x) dx = 0$$

$$2. \int_a^b f(x) dx = - \int_b^a f(x) dx$$

3. If $a \leq c \leq b$, then
$$\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx .$$

Examples: