

Week in Review # 3
Section 1.6, 1.7, and 1.8

Things to know:

- Know how to convert between the different bases of an exponential function.
 - Know the difference between continuous and relative rate of growth/decay.
 - Know how to simplify with logarithms
 - Know how to use logarithms to solve an exponential equation.
 - Understand what the different growth terms mean: half-life, doubling time,...
 - Understand the terms present value and future value of a payment.
 - Know how to shift and scale functions.
 - Know how to compose functions.
-

1. Simplify with logarithm rules.

(a) $\ln(x^4 z^5)$

(b) $\ln\left(\frac{e^{3x}}{x^5}\right)$

2. Solve for x.

(a) $J = 5 * 8^x$

(b) $8 * 3^x = 2 * 7^x$

3. For each of these formulas

I) Convert them into the form $y = P_0a^t$ or $y = P_0e^{kt}$

II) Give the relative rate of growth/decay.

III) Give the continuous rate of growth/decay.

(a) $y = 35(1.25)^t$

(b) $y = 27e^{-.127t}$

4. When solving for the yearly continuous rate of decay for a substance a student rounded the answer to two decimal places and got the answer of 2%.

(a) If the correct rate of decay was 1.505%, find the half-life of the substance.

(b) If the correct rate of decay was 2.4%, find the half-life of the substance.

(c) How does the half-life of the student's rate of decay compare with the answers in parts (a) and (b).

5. A bank account was started with \$600. Two years later the account had \$850.

(a) What is the continuous interest rate for the account?

(b) How long will it take for the account to triple?

6. You have been offered a payment of \$5000 in 4 years and a payment of \$8000 in 7 years. What is the present value of this offer if the interest rate is

(a) 6.25% compounded annually.

(b) 6.25% compounded continuously.

7. For the functions $f(x) = \sqrt{x+5}$ and $g(x) = 2x^2 + 3$ find

(a) $g(f(7)) =$

(b) $f(g(2)) =$

(c) $g(3 + g(1)) =$

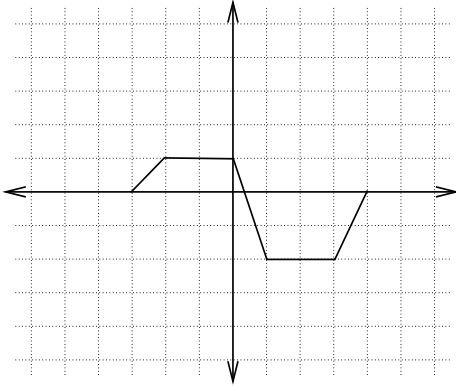
(d) $f(g(x)) =$

(e) $g(f(x)) =$

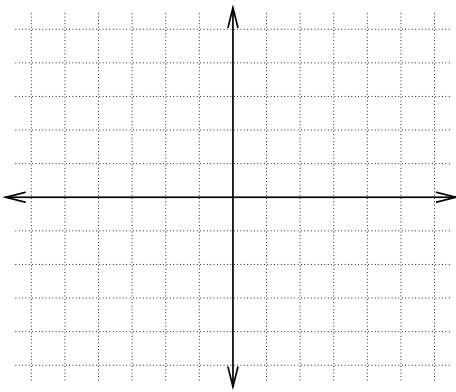
8. Find two function $f(x)$ and $g(x)$ such that $h(x) = f(g(x))$

$$h(x) = 5 \ln(3x^2 + 1)$$

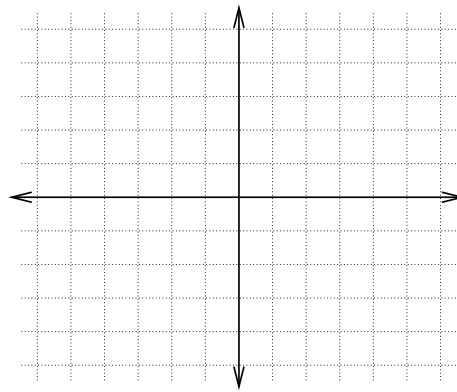
9. The graph of $f(x)$ is given. Use it to sketch the following.



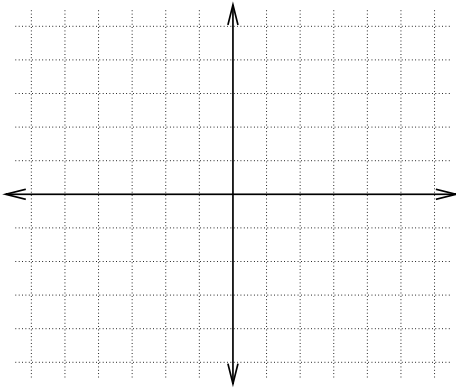
(a) $f(x+3)$



(b) $f(x)+2$



(c) $-2f(x)$



(d) $2 - f(x)$

