



Wir 5: Sections 14.5, 14.6

Section 14.5

- Problem 1.** If $z = \ln(9x - 6y)$, $x = \cos(e^t)$, $y = \sin^3(4t)$, find $\frac{dz}{dt}$.
- Problem 2.** If $w = u^2 + 2uv$, $u = r \ln s$, $v = 2r + s$, find $\frac{\partial w}{\partial r}$ and $\frac{\partial w}{\partial s}$.
- Problem 3.** If $z = x^4 + xy^3$, $x = uv^3 + w^4$, $y = u + ve^w$, find $\frac{\partial z}{\partial u}$ when $u = 1$, $v = 1$, $w = 0$.
- Problem 4.** The height and radius of a right circular cone are changing with respect to time. If the base radius of the cone is increasing at a rate of $\frac{1}{4}$ inches per minute while the height is decreasing at a rate $\frac{1}{10}$ inches per minute, find the rate in which the volume of the cone is changing when the radius of the cone is 2 inches and the height of the cone is 1 inch.
- Problem 5.** The length l , width w and height h of a box change with time. At a certain instant, the dimensions are $l = 1$ m, $w = 3$ m and $h = 2$ m, and l and w are increasing at rate of 2 m/s while h is decreasing at a rate of 3 m/s. At that same instant, find the rate at which the surface area is changing.

Section 14.6

- Problem 6.** $f(x, y) = xy \sin x$, find the directional derivative at the point $(\frac{\pi}{2}, -1)$ in the direction $\mathbf{u} = \left\langle \frac{3}{5}, \frac{4}{5} \right\rangle$.
- Problem 7.** Given $f(x, y) = x^3y^2$, find the directional derivative at the point $(-1, 2)$ in the direction $4\mathbf{i} - 3\mathbf{j}$.
- Problem 8.** If $f(x, y) = x^2e^{xy}$, find the rate of change of f at the point $(1, 0)$ in the direction of the point $P(1, 0)$ to the point $Q(5, 2)$.

With thanks to Amy Austin for generously sharing all of her WIR problems from last semester.



- Problem 9.** Find the gradient of $f(x, y) = x^2 + y^3 - 4xy$ at the point $(1, -1)$.
- Problem 10.** If $f(x, y) = x^2e^{-2y}$, $P(2, 0)$, $Q(-3, 1)$.
- Find the directional derivative at Q in the direction of P .
 - Find a vector in the direction in which f increases most rapidly at P , and find the rate of change of f in that direction.
- Problem 11.** Find the maximum rate of change of $f(x, y) = \sin^2(3x + 2y)$ at the point $\left(\frac{\pi}{6}, -\frac{\pi}{8}\right)$ and the direction in which it occurs.
- Problem 12.** Find the equation of the tangent plane to the surface $f(x, y) = x^2 + y^2 - 4xy$ at the point $(1, 2)$.