Honors Math 142

| Section | Problems |
| :--- | :--- |
| 1.1 | $3-51,56-65$ |
| 1.2 | $5-9,11,12,16-28,32,33,38-50,55-59,60-62($ parts a, b and c only $)$ |
|  | $63-68,75($ parts a-d), 76-79 |
| 1.3 | $5-46$ |
| 1.4 | $2,4,5,7,9,11,13-17,24-27,29-34,36-39,44-47,50-57,60-63$, |
|  | $67-71$ |
| 1.5 | $1-21,23-33$ odd, $43,44,47,51,53-57,63,64,68,69,70$ |
| 1.6 | $1-20,25-29,31,32,35,36,37,40,41,45,46,47,53-55$ |
| $1.7^{*}$ | $1-4,5-12($ also give the domain $), 21-27,31-35,43-60,63$ |
| $1.8^{*}$ | $1-15$ |
| 2.1 | $5,6,9,10,19-46,50-53,57,58,59,61,62$ |
| 2.2 | $3-6,9-24,29-54$ |
| 2.3 | $8-12,27,28,29,31,33-41,45,55,56,57,65-70,73,74,76,77$ |
| 2.4 | $17-67,78,79$ |
| 2.5 | $1-47,53,55$ |
| 2.6 | $5-8,19-46$ |
| 3.2 | $3-25$ |
| 4.1 | $1-68$ |
| 4.2 | $1-47$ |
| 4.3 | $1-52$ |
| 4.5 | $5-12,13-21($ odd $), 23-28,32-36,39-46$ |
| 5.1 | $1-44,51,52,54,57-61$ |
| $*$ | See the additional problems for this section. |
|  |  |

## Additional Problems for Section 1.7

1. Solve for x .
(a) $5 * 10^{5 x}=3$
(b) $6=2 * 10^{-3 x}$
(c) $5 e^{3.1 x}=25$
(d) $\log 10^{x}=4$
(e) $\ln (4-x)=\frac{1}{2}$
(f) $\ln \left(x^{2}-3\right)=0$
(g) $2 \log (2 x+5)+6=0$
(h) $\ln (\ln 3 x)=0$
(i) $\ln (x+3)+\ln (x-3)=\ln (7)$
(j) $\log (x-2)+\log (x+4)=\log 7$
(k) $\log _{x}(15-2 x)=2$
(l) $\log _{x}(12 x-20)=2$
2. Use the properties of logarithms to rewrite the following as the sum and/or difference of logarithms
(a) $\ln (x+5)^{4} e^{5}$
(b) $\log \left(\frac{100 x^{4}}{y^{3}}\right)$
(c) $\log _{5}\left(\frac{x+3}{y^{4} z^{2}}\right)$
3. Write as a single logarithm.
(a) $7 \log (x+5)+2 \log (x+1)$
(b) $\log _{2} x+5 \log _{2}(y+1)+2 \log _{2}(z-1)$
(c) $2 \ln (x+4)-5 \ln y+3 \ln z$
4. In 1969, all field goal attempts and successes were analyzed in the National Football League and American Football League. The percentages of success are shown in the table. (The data has been summarized: all tries between 10 and 19 yards from the goal are listed as 14.5 yards out. etc. $)^{1}$

| Distance | 14.5 | 24.5 | 34.5 | 44.5 | 52 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Fraction of tries that were successful | 0.9 | 0.75 | 0.54 | 0.29 | 0.15 |

(a) Discuss whether a linear or exponential model fits best.
(b) For the exponential graph, what success rate does this function predict from a distance of 50 yards?
(c) For the exponential graph, what is the distance that would have a success rate of 0.5 ?
(d) Is there a better model for this data?
2. The size of the average farm in the United States has been growing steadily over the years. The accompanying data, obtained from the U.S. Department of Agriculture, gives the size of the average farm(in acres) from 1940 to 1997. ${ }^{2}$

| Year | 1940 | 1950 | 1960 | 1970 | 1980 | 1997 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Avg. Size(acres) | 168 | 213 | 297 | 374 | 427 | 471 |

(a) What regression model would be good to use with this data? Explain.
(b) Using your model, what was the size of the average farm in 1985 ?
(c) In what year was the size of the average farm 435 acres?
3. The table lists the total (cumulative) number of AIDS cases (in thousands) diagnosed in the United States up to 1996. For example, a total of 22,620 AIDS cases were diagnosed between 1981 and $1985 .{ }^{3}$ When you put the data in the calculator, let time start in 1980 , i.e. $\mathrm{x}=0$ is 1980 .

| Year | AIDS Cases | Year | AIDS Cases |
| :---: | :---: | :---: | :---: |
| 1982 | 1.563 | 1990 | 193.245 |
| 1983 | 4.647 | 1991 | 248.023 |
| 1984 | 10.845 | 1992 | 315.329 |
| 1985 | 22.620 | 1993 | 361.509 |
| 1986 | 41.662 | 1994 | 441.406 |
| 1987 | 70.222 | 1995 | 515.586 |
| 1988 | 105.489 | 1996 | 584.394 |
| 1989 | 147.170 |  |  |

(a) What regression model would model the data best? Explain.
(b) In what year would the total number of AIDS cases diagnosed go above 1 million?
4. The number of abandoned cars in New York City has dropped in recent years because of reduced auto theft and increasing scrap metal prices. The following table, based on estimates from a graph in The New York Times, gives the number of abandoned cars as a function of the year. ${ }^{4}$ let time start in 1986, i.e. 1986 is $\mathrm{x}=0$.

| Year | 1986 | 1987 | 1988 | 1989 | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Abandoned Cars(1000s) | 82 | 120 | 140 | 148 | 135 | 95 | 75 | 51 | 38 | 27 | 20 |

What regression model would model the data best? Explain.

[^0]Compute these limits $\lim _{x \rightarrow a^{-}} f(x), \lim _{x \rightarrow a^{+}} f(x)$, and $\lim _{x \rightarrow a} f(x)$ at the indicated value, $a$, for each of these functions.

1. $a=1, f(x)= \begin{cases}3 x-4 & \text { if } x \leq 1 \\ 7-2 x & \text { if } x>1\end{cases}$
2. $a=0, f(x)= \begin{cases}x^{4}-x+1, & \text { if } x<0 \\ x^{2}-4 x+1, & \text { if } x \geq 0\end{cases}$
3. $a=0, f(x)= \begin{cases}x^{4}-x+1, & \text { if } x<0 \\ 4, & \text { if } x=0 \\ x^{2}-4 x+1, & \text { if } x>0\end{cases}$
4. $a=-1, f(x)= \begin{cases}3 x+6, & \text { if } x<-1 \\ x^{2}-1, & \text { if }-1 \leq x<2 \\ 3 x^{2}-5 x+1, & \text { if } x \geq 2\end{cases}$
5. $a=2, f(x)= \begin{cases}3 x+6, & \text { if } x<-1 \\ x^{2}-1, & \text { if }-1 \leq x<2 \\ 3 x^{2}-5 x+1, & \text { if } x \geq 2\end{cases}$
6. $a=1, f(x)= \begin{cases}-x+1, & \text { if } x<1 \\ \frac{2}{1-x}, & \text { if } x>1\end{cases}$
7. $a=2, f(x)= \begin{cases}\frac{-1}{x-2}, & \text { if } x>2 \\ \frac{4}{2-x}, & \text { if } x<2\end{cases}$

[^0]:    ${ }^{1}$ Applied Calculus, abridged. by Hughes-Hallett/Gleason/Lock/Flath/et al. pg 110
    ${ }^{2}$ Finite Mathematics, 7 th ed. by Tan. pg. 60
    ${ }^{3}$ Finite Mathematics and Calculus, 6th ed. by Lial, Greenwell and Ritchey. pg. 513
    ${ }^{4}$ Finite Mathematics and Calculus, 6th ed. by Lial, Greenwell and Ritchey. pg. 528

