

LAPLACE TRANSFORM TABLE

$$\begin{aligned} \mathcal{L}\{1\}(s) &= \frac{1}{s} & \mathcal{L}\{\cos bt\}(s) &= \frac{s}{s^2 + b^2} \\ \mathcal{L}\{e^{at}\}(s) &= \frac{1}{s - a} & \mathcal{L}\{e^{at}t^n\}(s) &= \frac{n!}{(s - a)^{n+1}}, \quad n = 1, 2, \dots \\ \mathcal{L}\{t^n\}(s) &= \frac{n!}{s^{n+1}}, \quad n = 1, 2, \dots & \mathcal{L}\{e^{at} \sin bt\}(s) &= \frac{b}{(s - a)^2 + b^2} \\ \mathcal{L}\{\sin bt\}(s) &= \frac{b}{s^2 + b^2} & \mathcal{L}\{e^{at} \cos bt\}(s) &= \frac{s - a}{(s - a)^2 + b^2} \end{aligned}$$

$$\mathcal{L}\{f + g\} = \mathcal{L}\{f\} + \mathcal{L}\{g\}$$

$$\mathcal{L}\{cf\} = c\mathcal{L}\{f\} \quad \text{for any constant } c$$

$$\mathcal{L}\{e^{at}f(t)\}(s) = \mathcal{L}\{f\}(s - a)$$

$$\mathcal{L}\{f'\}(s) = s\mathcal{L}\{f\}(s) - f(0)$$

$$\mathcal{L}\{f''\}(s) = s^2\mathcal{L}\{f\}(s) - sf(0) - f'(0)$$

$$\mathcal{L}\{f^{(n)}\}(s) = s^n\mathcal{L}\{f\}(s) - s^{n-1}f(0) - s^{n-2}f'(0) - \dots - f^{(n-1)}(0)$$

$$\mathcal{L}\{t^n f(t)\}(s) = (-1)^n \frac{d^n}{ds^n} (\mathcal{L}\{f\}(s))$$

$$\mathcal{L}\{f(t - a)u(t - a)\}(s) = e^{-as} \mathcal{L}\{f(t)\}(s)$$

$$\mathcal{L}\{g(t)u(t - a)\}(s) = e^{-as} \mathcal{L}\{g(t + a)\}(s)$$

$$\mathcal{L}\{f\}(s) = \frac{\int_0^T e^{-st} f(t) dt}{1 - e^{-sT}} \quad \text{for } f \text{ of period } T$$

$$\mathcal{L}\{f * g\}(s) = (\mathcal{L}\{f\}(s))(\mathcal{L}\{g\}(s))$$