

Math 365 Lecture Notes Section 5.1 – The Set of Rational Numbers

★ Definitions

- 1) Rational Number –
- 2) Numerator –
- 3) Denominator –
- 4) Fraction –
- 5) Proper Fraction –
- 6) Improper Fraction –

★ Early Fractions

- 1) Egyptians used fractions in the form $\frac{1}{a}$
- 2) Babylonian notation for fractions:
- 3) Note the similarity to $23^\circ 42' 16''$
- 4) $\frac{a}{b}$ as a fraction with the fraction bar is of Hindu origin

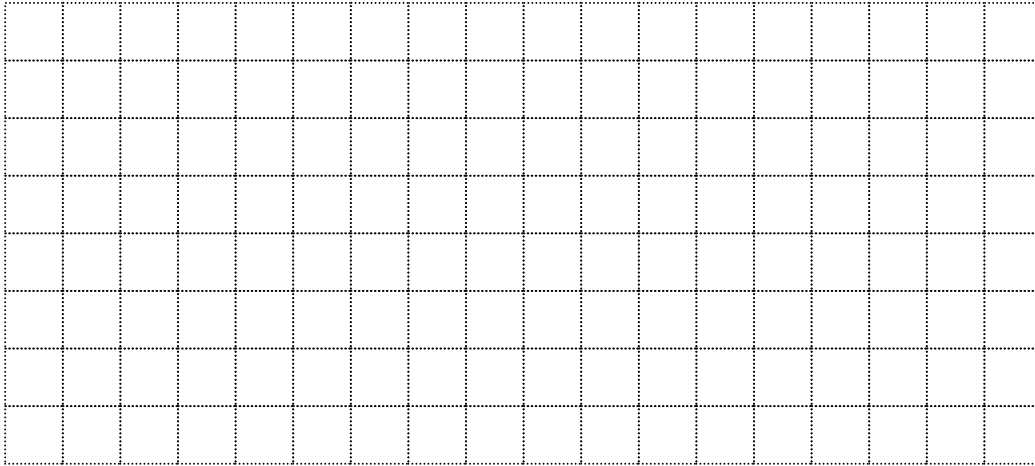
★ Ways to Use Fractions

- 1) Division problem:
- 2) Part of a whole:
- 3) Ratio:
- 4) Probability:

★ Fundamental Law of Fractions:

$\frac{a}{b}$ is any fraction and $n \neq 0$, then $\frac{a}{b} = \frac{an}{bn}$

★ **Activity 1**



★ **Activity 2**

By the end of this section you should be able to:

1. Explain the meaning of a/b .
2. Solve equations with fractions
3. Simplify Fractions

★ **Solve equations with fractions**

1) Use the Fundamental Law of Fractions to rewrite each fraction with the same denominator.

2) Simplify fractions by factoring

3) Simplest Form:

4) Practice Problems

a. $\frac{x^2 + x}{x + x^3}$

b. $\frac{5 + 5x}{5x^2}$

c. $\frac{a^2 - b^2}{a - b}$

★ Showing two fractions are equal

- 1) Write both fractions in simplest form

- 2) Rewrite fractions with the least common denominator

- 3) Rewrite fractions with “any” common denominator

★ Properties and Theorems:

★ Ordering fractions

★ Denseness Property

- 1) definition

- 2) example:
 - a. Find two fractions between $\frac{5}{12}$ and $\frac{3}{4}$.

 - b. Find two fractions between $\frac{2}{3}$ and $\frac{3}{4}$.

 - c. Alternate solution to part b above: