

1. What is the distance between $\frac{-7}{4}$ and 2?

$$2. \left(\frac{81x^{-8}}{16y^2z^{-4}} \right)^{\frac{3}{4}} =$$

3. Fully factor $2x^4 - 6x^3 - 2x + 6$.

$$4. \frac{1 + \frac{2}{x}}{\frac{x}{5} - 1} =$$

$$5. \left| (\overline{2i-4})(i^2-9i) \right| =$$

6. Solve $\sqrt{36-x} = 24-x$.

$$7. \text{Solve } \frac{3x^2 - 13x + 8}{5-x} \geq 4$$

8. Find the standard equation of the circle whose center is the midpoint of the line segment whose endpoints are $(6, -3)$ and $(12, -8)$ and whose diameter is 7.

9. Test $5xy - 6x^3y^4 = 30x$ for y -axis symmetry.

10. Find the slope-intercept form of the line that passes through point $(-8, 4)$ and that is perpendicular to the line $5x - 6y = 20$.

11. If $f(x) = \frac{2x^2}{3x-5}$, evaluate and simplify the difference quotient.

12. A full 200-ml beaker contains a 38% concentration of saline solution. How much of the mixture should be poured off and replaced with pure water to reduce the salinity concentration to 25%?

13. Where is the function f increasing, decreasing, and constant? What is its minimum value? Evaluate $f(-8)$.

$$f(x) = \begin{cases} 5, & x < -8 \\ -2x, & -8 \leq x < -3 \\ \sqrt{x+4}, & x \geq 0 \end{cases}$$

14. $\sqrt{x^2} =$

15. Write $f(x) = -5x^2 + 15x - \frac{53}{4}$ in standard form. Identify the vertex and zeros (real and complex) of f , and the transformations of $g(x) = x^2$ needed to obtain the graph of f .

16. If $f(x) = \frac{-2}{x^2 - 1}$, $g(x) = 3\sqrt{x}$ and $h(x) = x + 1$, evaluate $((f \circ g) - h)(x)$ and find its domain.

17. If $f(x) = 2\log_3\left[\frac{1}{4}(x-5)\right]$, find its inverse function (complete with domain and range).

18. Describe the end behavior of the polynomial $f(x) = -99x^{34} + 78x^{27} - 5x^2 + 2$.

19. Find the domain, holes (if any), intercepts, vertical asymptotes and horizontal asymptotes of

the function $f(x) = \frac{(4x+12)(x^2-1)}{(x-5)(x+1)^2}$.

20. Solve the equation $6e^{8-2x} - 3 = 9$ for x .

21. (2 ways to solve) $\log_3 1 - \log_3 81 =$

22. What is the domain, in interval notation, of the function $f(x) = \frac{\sqrt{x^2 - 9}}{\log_2(12 - x)}$?

23. Solve $\log_2(5 - x) = 3 - \log_2(x + 4)$ for x .

24. A radioactive sample decayed 40% after 3 years. What is its half-life, both exact and as an approximation to 2 decimal places? How much of a 10 gram sample will remain after 2 years, both exact and as an approximation to 2 decimal places?

25. Algebraically solve the system of equations.

$$5x + 6y = 30$$

$$6y = 2x + 9$$

26. Algebraically solve the system of equations.

$$y - 20 = -(x - 5)^2$$

$$2(x - 5)^2 + y^2 = 64$$

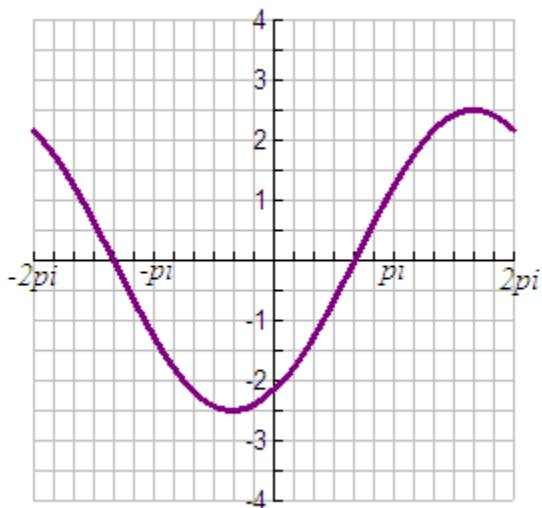
27. If a circle has a 16-meter diameter, find the exact arc length and sector area subtended by a central angle of $\frac{5\pi}{6}$.

28. $\tan \frac{2\pi}{3} =$

29. $\csc \frac{3\pi}{2} =$

30. If $\cot \theta = \frac{3}{10}$ and $\csc \theta < 0$, exactly evaluate $\sin 2\theta$.

31. Write a function of the form (a) $f(x) = a \sin k(x-b)$ and then (b) $f(x) = a \cos k(x-b)$ whose graph is shown below, where a , k , and b are positive and b is as small as possible.



32. Exactly evaluate $\cos \frac{13\pi}{12}$.

33. $\sin\left(\sin^{-1}\left(\frac{1}{2}\right) + \sin^{-1}\left(\frac{4}{5}\right)\right) =$

34. $\cos^{-1}\left(\cos\frac{5\pi}{4}\right) =$

35. If $B = 45^\circ$, $c = 40$ meters, and $b = 64$ meters, solve the triangle.

36. Find the three angles of a triangle whose sides have length of 3 meters, 6 meters, and 8 meters.

37. Solve $\sin 2x - 2\sin x + \cos x - 1 = 0$ on the interval $[0, 2\pi)$.

38. Represent the vector from $P(-1, 3, 0)$ to $Q(9, -6, -5)$.

39. $\langle -3, 7, -1 \rangle - 2\langle 8, -4, -3 \rangle =$

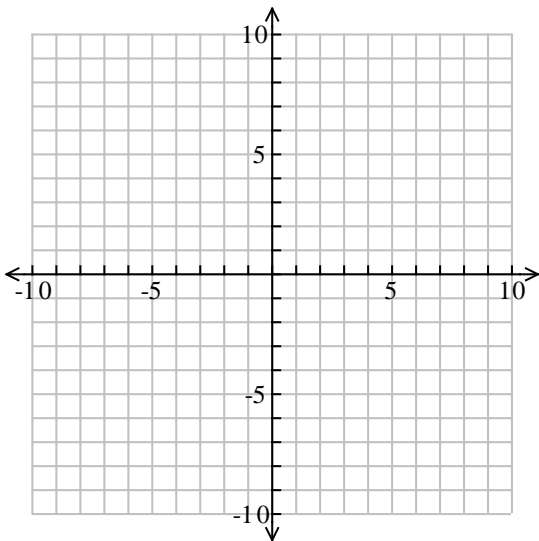
40. Find the unit vector in the direction of $\langle -3, 7 \rangle$.

41. $2\langle -3, 7, -1 \rangle \bullet \langle 8, -4, -3 \rangle =$

42. Find the angle between $\langle 2, -8 \rangle$ and $\langle -4, 5 \rangle$.

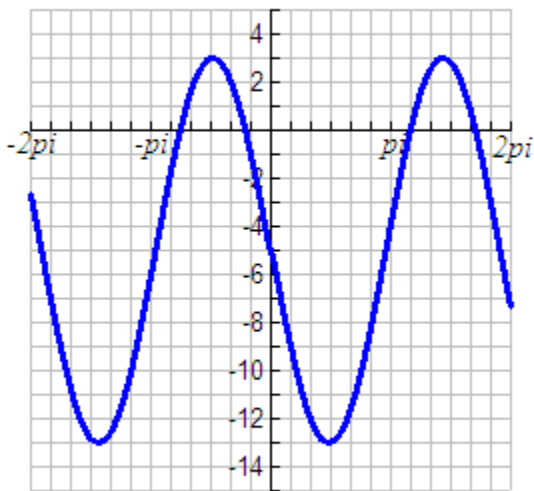
43. Find the center and radius of the circle $-5x^2 - 5y^2 + 4x - 15y + 12 = 0$.

44. Sketch an even function that satisfies **all** of the following: is decreasing on the interval $(2, 7)$; is increasing on the intervals $(0, 1)$, $(1, 2)$ and $(7, \infty)$; has x -intercepts at 4 and 8; has a y -intercept of 5; has a minimum value of -9 and is undefined at $x = 1$.



45. If $\log_n 2 = p$, $\log_n 3 = q$, and $\log_n 5 = r$, find the value of $\log_n \frac{144}{1500}$ in terms of p , q , and r .

46. Below is the graph of a sine function that has no phase shift. Use the graph to find each of the following.



- Amplitude:
- Period:
- Vertical Shift:
- Reflection about the (circle one): x-axis y-axis line $y = x$
- Equation for this Sine Function: