

Due Thursday 03/20/14 at the beginning of class.

**STAPLE YOUR WORK**

## QUIZ 7 (Take-home) MATH 221

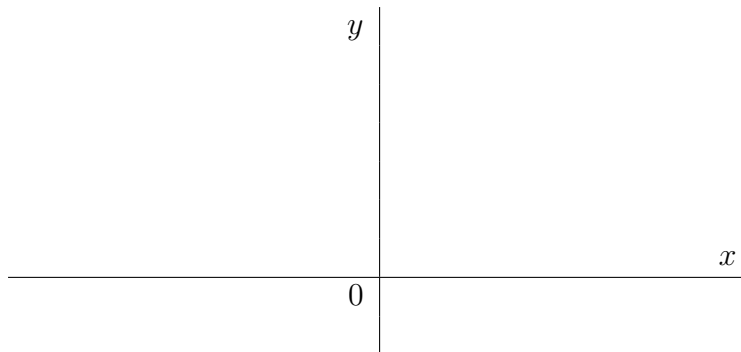
LAST NAME \_\_\_\_\_ FIRST NAME \_\_\_\_\_

On my honor, as an Aggie, I certify that the solution submitted by me is my own work. I had neither given nor received unauthorized aid on this work.

Signature: \_\_\_\_\_

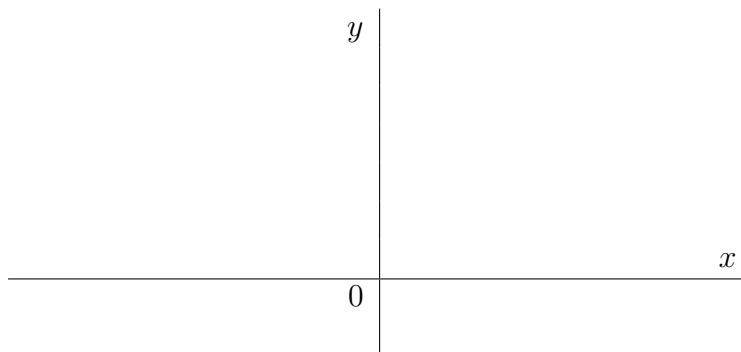
1. [20pts] Given

$$\iint_D f(x, y) \, dA = \int_0^1 \int_{-\sqrt{1-y^2}}^{2(1-y)} f(x, y) \, dx \, dy$$

(a) Sketch the region of integration  $D$ .(b) Reverse the order of integration. *WRITE YOUR ANSWER HERE:*


2. [20pts] Given

$$\int_0^2 \int_{-\sqrt{1-(y-1)^2}}^{(2-y)/2} f(x, y) \, dx \, dy.$$

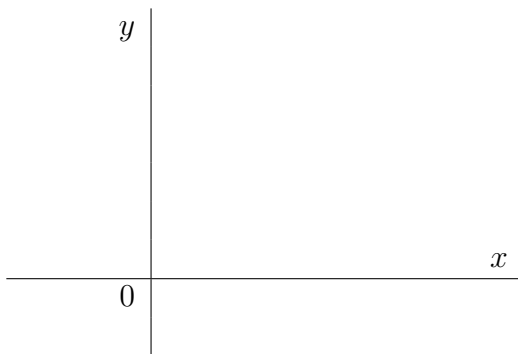
(a) Sketch the region of integration  $D$ .(b) Reverse the order of integration. *WRITE YOUR ANSWER HERE:*

3. [20pts] Evaluate the integral by reversing the order of integration:

$$\int_0^3 \int_{y^2}^9 y \cos(x^2) dx dy.$$

4. [20pts] Find the volume of the solid that lies under the surface  $z = 3xy$  and above the region  $D$  in the  $xy$ -plane bounded by the parabolas  $y = x^2$  and  $x = y^2$ .

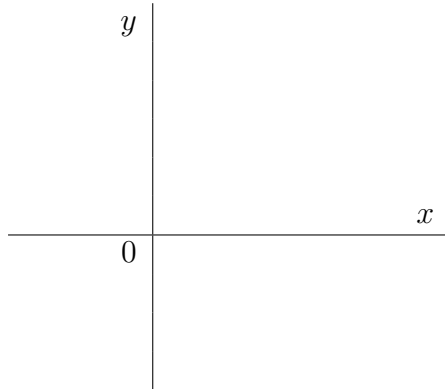
*Sketch  $D$  here:*



5. [20pts] A lamina occupies the region  $D = \{(x, y) | 1 \leq x^2 + y^2 \leq 4, x \geq 0\}$ . The density of the lamina at any point is equal to its distance from the origin.

(a) Find the mass of the lamina.

*Sketch  $D$  here:*



(b) Find the center of mass of the lamina.