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Math 220 – Homework 12 HNR

- 1. Let a = -255 and b = 143
 - (a) Use the Euclidean Algorithm to determine gcd(a, b).
 - (b) Find integers x and y such that $ax + by = \gcd(a, b)$.
- 2. (a) Write the integer 42750 in a compact standard form.
 - (b) Determine the following, representing your answer in the compact standard form:

$$\gcd(2^{2018} \cdot 3^4 \cdot 55 \cdot 7^2, 6 \cdot 3^2 \cdot 77)$$

- 3. Prove that if p is a prime number greater than 3, then p is of the form 3k + 1 or 3k + 2.
- 4. Prove that if p is a prime number, then $\sqrt[n]{p}$ is irrational for every integer $n \geq 2$.
- 5. Prove or disprove that 3 is the only prime number of the form $n^2 1$.
- 6. Prove that if a is a positive integer of the form 3n+2, then at least one prime divisor of a is of the form 3n+2.
- 7. Let $a, b \in \mathbb{Z}$ with a and b not both zero. Prove that if $d = \gcd(a, b)$, then $\gcd\left(\frac{a}{d}, \frac{b}{d}\right) = 1$.