Math 220/903&904-Homework 3

Due Wednesday 09/30 at the beginning of class

PART A

Problems from the textbook:

Section 2.1 # 1(b, c, e, i); 2(b, f,h); 4(b,c,f,i); 5; 7(e, f, h); 8(b,c, d); 13; 14; 15; 19(b, c); 20(c, f).

Section 2.2 # 4(b, e), 5(b, e), 6,

PART B

- 1. Determine the truth or falsehood of the following statements.
 - (a) The contrapositive of the statement

"If all elements of A are elements of B, then A is a subset of B"

is the statement

"If A is a subset of B, then all elements of A are elements of B".

- (b) $\{a,b\} = \{b,a,b\}$
- (c) $\{x \in \mathbb{N} | -x \in \mathbb{N}\} = \emptyset$.
- (d) If $A = \{m \in \mathbb{Z} | 2 < m \le 5\}$ then |A| = 4.
- (e) The empty set is a subset of every set except itself.
- 2. Let A, B, and C be nonempty sets. Determine the truth or falsehood of the following statements. (Write TRUE or FALSE for each statement.)
 - (a) $A A = \emptyset$.
 - (b) $A \subset A$.
 - (c) A B = C B implies A = C.
 - (d) If A is not a subset of B and B is not a subset of A, then $A \cap B = \emptyset$.
 - (e) $A \cup (B \cap C) = (A \cap C) \cup (B \cap C)$.
 - (f) $A \cup A = A \cap A$ for all sets A.
- 3. Let $U = \{x, y, 1, 2, 3\}$ be the universal set and let $A = \{x, y, 1, 2\}$, $B = \{2, 3\}$, $C = \{1, 3, x, y\}$. Determine the following (show all intermediate steps):
 - (a) $\overline{A} \cup (B \cap C)$
 - (b) $\overline{B \cup C} \cap U$
 - (c) $\overline{(A \cup B) (B \cap C)}$
- 4. Disprove the following statement:

''Let A,B, and C be nonempty subsets of a universal set U. Then $A\cap B=A\cap C$ implies B=C.''

- 5. Let $U = \mathbb{R}$ be the universal set. Consider $A = \{x \in \mathbb{R} | |2x + 3| \ge 7\}$ and $B = \{x \in \mathbb{R} | |x| \le 1\}$.
 - (a) Express the sets A and B using interval notation (as an interval or a union of intervals).
 - (b) Determine $\overline{A} \cap B$ as an interval or a union of intervals.