

1. Know the following definitions and theorems:
  - a. order of a differential equation,
  - b. linear differential equation
  - c. homogeneous, non-homogeneous, autonomous
  - d. existence uniqueness theorem for first order differential equations,
  - e. exact and separable first order equations,
  - f. phase line for an autonomous first order differential equation
  - g. Wronskian, linearly independent functions on an interval,
  - h. characteristic equation of a second order linear constant coefficient differential equation,
  - i. phase plane for a system of two first order autonomous differential equations in two unknown functions,
  - j. definition of linearity for a system of differential equations,
  - k. eigenvalues and eigenvectors,
  - l. linearly independent vectors,
  - m. linearly independent set of vector valued functions on an interval  $[a, b]$ ,
  - n. Wronskian of a set of vector valued functions,
  - o. fundamental solution set,
  - p. existence-uniqueness theorem for a first order system of differential equations,
  - q. equilibrium points,
  - r. Laplace transform,
  - s. convolution of two functions,
  - t. convolution theorem,
  - u. properties of the Dirac delta function,
  - v. singular and regular singular points of a second order differential equation.

2. You should be able to do the following:
  - a. solve mixing problems and population growth problems,
  - b. find exact solutions to first order linear and separable differential equations,
  - c. find exact solutions to second order linear constant coefficient differential equations,
  - d. know how to solve Cauchy-Euler second order differential equations,
  - e. reduction of order technique, which is used to find a second solution to a DE,
  - f. variation of parameters, which is used to find a particular solution to a non-homogeneous DE,
  - g. sketch a few lines in a phase plane,
  - h. find eigenvalues and eigenvectors of  $2 \times 2$  matrices,
  - i. construct a fundamental solution set for linear constant coefficient systems of differential equations, and the general solution to such a system,
  - j. solve an initial value problem for a constant coefficient first order system,
  - k. be able to use the Laplace transform to convert a differential equation into an algebraic equation,
  - l. use the table of Laplace transforms to compute the inverse Laplace transform of a function,
  - m. use the definition of Laplace transform to verify any of the formulas in the table of transforms,
  - n. compute the convolution of two functions,
  - o. use the delta function to model an impulse force,
  - p. find power series solution of a second order differential equation around an ordinary point.
  - q. find a power series solution of a second order differential equation around a regular singular point using the method of Frobenius.