

### Third Writing Assignment, Math220

Prove the following

- (1) Let  $a, b, c, d$  and  $n$  be integers with  $n > 0$ . If  $a \equiv b \pmod{n}$  and  $c \equiv d \pmod{n}$ , then  $ac \equiv bd \pmod{n}$ .
- (2) Let  $a, b$  and  $n$  be integers with  $n > 0$ . If  $a \equiv b \pmod{n}$ , then  $a^3 \equiv b^3 \pmod{n}$ .
- (3) Let  $a, b, k$  and  $n$  be integers with  $n > 0$  and  $k > 0$ . If  $a \equiv b \pmod{n}$ , then  $a^k \equiv b^k \pmod{n}$ .
- (4) Prove or find a counterexample: Let  $a, b, c$  and  $n$  be integers with  $n > 0$ . If  $ac \equiv bc \pmod{n}$ , does it follow that  $a \equiv b \pmod{n}$ .