

**MATH 151, FALL 2013
COMMON EXAM II - VERSION A**

LAST NAME: _____ FIRST NAME: _____

INSTRUCTOR: _____

SECTION NUMBER: _____

UIN: _____

DIRECTIONS:

1. The use of a calculator, laptop or computer is prohibited.
2. TURN OFF cell phones and put them away. If a cell phone is seen during the exam, your exam will be collected and you will receive a zero.
3. In Part 1 (Problems 1-15), mark the correct choice on your ScanTron using a No. 2 pencil. The ScanTron will not be returned, therefore *for your own records, also record your choices on your exam!* Each problem is worth 3 points.
4. In Part 2 (Problems 16-21), present your solutions in the space provided. *Show all your work* neatly and concisely and *clearly indicate your final answer*. You will be graded not merely on the final answer, but also on the quality and correctness of the work leading up to it.
5. Be sure to *write your name, section number and version letter of the exam on the ScanTron form.*

THE AGGIE CODE OF HONOR

“An Aggie does not lie, cheat or steal, or tolerate those who do.”

Signature: _____

DO NOT WRITE BELOW!

Question	Points Awarded	Points
1-15		45
16		10
17		6
18		12
19		12
20		8
21		7
		100

PART I: Multiple Choice. 3 points each

- Find $\lim_{t \rightarrow 0} \frac{\sin^2(6t)}{4t^2}$.
 - $\frac{3}{2}$
 - 9
 - $\frac{1}{9}$
 - 0
 - ∞
- If $g(x) = xf(x^3)$, $f(2) = 4$, $f(8) = 3$, $f'(8) = -1$, and $f'(2) = -2$, what is $g'(2)$?
 - 24
 - 12
 - 16
 - 21
 - 44
- Find the slope of the tangent line to the curve $x^3 + y^3 = x^2 + 5y$ at the point $(2, 1)$.
 - $m = 4$
 - $m = -1$
 - $m = \frac{11}{5}$
 - $m = 2$
 - $m = \frac{1}{4}$
- Use differentials to approximate $\sqrt[3]{8.2}$.
 - $\sqrt[3]{8.2} \approx \frac{61}{60}$
 - $\sqrt[3]{8.2} \approx \frac{22}{5}$
 - $\sqrt[3]{8.2} \approx \frac{119}{60}$
 - $\sqrt[3]{8.2} \approx \frac{11}{5}$
 - $\sqrt[3]{8.2} \approx \frac{121}{60}$

5. Find $\lim_{x \rightarrow \infty} \frac{2^x + 2^{-4x}}{7(2^x) - 2^{-4x}}$.

(a) $\frac{2}{7}$

(b) $\frac{1}{7}$

(c) ∞

(d) 0

(e) -1

6. The function $f(x) = 4x + \sin x$ is a one-to-one function. If g is the inverse of f , what is $g'(4\pi)$?

(a) $-\frac{1}{5}$

(b) -1

(c) $\frac{1}{5}$

(d) $\frac{1}{4}$

(e) $\frac{1}{3}$

7. Consider the parametric curve $x(t) = t^4 + 1$ and $y(t) = \cos\left(\frac{\pi}{2}t\right)$. Find the slope of the tangent line at the point $(2, 0)$.

(a) $-\frac{\pi}{8}$

(b) $-\frac{1}{4}$

(c) $-\frac{8}{\pi}$

(d) 0

(e) $-\frac{\pi}{4}$

8. Find $h''(1)$ if $h(x) = e^{-x^2}$.

(a) $\frac{4}{e}$

(b) $\frac{2}{e}$

(c) $-\frac{2}{e}$

(d) $\frac{1}{e}$

(e) $-\frac{4}{e}$

9. $\lim_{x \rightarrow 2^-} \left(\frac{1}{4}\right)^{\frac{x}{x-2}}$

- (a) 0
- (b) $-\infty$
- (c) $\frac{1}{4}$
- (d) 1
- (e) ∞

10. At what point on the curve $x = 2t^2 - 4t$, $y = t^2 - t$ is the tangent line horizontal?

- (a) $(-1, 0)$
- (b) $\left(\frac{1}{2}, -\frac{1}{4}\right)$
- (c) $(0, 0)$
- (d) $\left(-\frac{3}{2}, -\frac{1}{4}\right)$
- (e) $(-2, 0)$

11. Find the equation of the tangent line to the curve $g(x) = \frac{x}{2x+1}$ at $x = 4$.

- (a) $y - \frac{4}{9} = \frac{1}{2}(x - 4)$
- (b) $y - \frac{4}{9} = \frac{1}{81}(x - 4)$
- (c) $y = \frac{1}{81}(x - 4)$
- (d) $y - \frac{4}{3} = \frac{1}{81}(x - 4)$
- (e) $y - \frac{4}{9} = \frac{1}{9}(x - 4)$

12. Find the quadratic approximation for $f(x) = e^{4x}$ at $x = 0$.

- (a) $Q(x) = 1 + 4x + 16x^2$
- (b) $Q(x) = 1 + x + \frac{1}{2}x^2$
- (c) $Q(x) = 1 + x + x^2$
- (d) $Q(x) = 1 + 4x + 8x^2$
- (e) $Q(x) = 1 + 4x + 2x^2$

13. An object is moving according to the equation of motion $s(t) = \cos t + \frac{1}{4}t^2$. Find the time(s) when the acceleration is zero for $0 \leq t \leq 2\pi$.

(a) $t = \frac{2\pi}{3}, t = \frac{4\pi}{3}$

(b) $t = \frac{\pi}{6}, t = \frac{11\pi}{6}$

(c) $t = \frac{5\pi}{6}, t = \frac{7\pi}{6}$

(d) $t = \frac{\pi}{4}, t = \frac{7\pi}{4}$

(e) $t = \frac{\pi}{3}, t = \frac{5\pi}{3}$

14. Find the value(s) of x where the tangent line to the graph of $f(x) = x\sqrt{x}$ is parallel to the line $2x - 4y = 18$.

(a) $x = 9$

(b) $x = \pm 9$

(c) $x = \frac{16}{3}$

(d) $x = \frac{1}{9}$

(e) $x = \pm \frac{1}{9}$

15. Find the unit tangent vector to the curve $\mathbf{r}(t) = \langle \sin(3t), \cos(3t) \rangle$ at $t = \frac{\pi}{9}$.

(a) $\left\langle -\frac{1}{2}, \frac{\sqrt{3}}{2} \right\rangle$

(b) $\left\langle \frac{\sqrt{3}}{2}, -\frac{1}{2} \right\rangle$

(c) $\left\langle \frac{1}{2}, -\frac{\sqrt{3}}{2} \right\rangle$

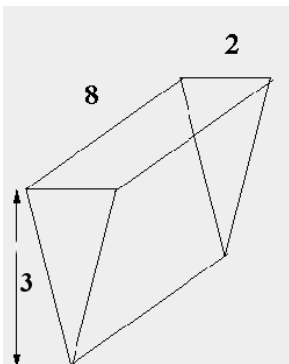
(d) $\left\langle -\frac{\sqrt{3}}{2}, \frac{1}{2} \right\rangle$

(e) $\left\langle -\frac{\sqrt{3}}{2}, -\frac{1}{2} \right\rangle$

PART II: Work Out

Directions: Present your solutions in the space provided. *Show all your work* neatly and concisely and *Box your final answer*. You will be graded not merely on the final answer, but also on the quality and correctness of the work leading up to it.

16. (10 pts) A trough is 8 feet long. The ends of the trough are isosceles triangles with height 3 feet and width 2 feet across the top. If water is being poured into the trough at a rate of 2 cubic feet per minute, how fast is the water level rising when the depth of the water is 1 foot?



17. (6 pts) Find $\frac{dy}{dx}$ if $y = e^{3xy}$.

18. Find the derivative of the following functions. Do not simplify.

a.) (4 pts) $f(x) = ((x^2 + 3)^5 + x)^8$

b.) (4 pts) $g(x) = \tan(\sqrt{x^2 + 3x})$

c.) (4 pts) $h(x) = \cos^4\left(a^3 + \frac{1}{x^2}\right)$

19. Given that $h(5) = 3$, $h'(5) = -2$, $g(5) = -3$ and $g'(5) = 6$, find $f'(5)$ for each of the following, if possible. If it is not possible, state what additional information is required.

a.) (3 pts) $f(x) = g(x)h(x)$

b.) (3 pts) $f(x) = \frac{g(x)}{h(x)}$

c.) (3 pts) $f(x) = [g(x)]^3$

d.) (3 pts) $f(x) = g(h(x))$

20. Consider the vector equation $\mathbf{r}(t) = \left\langle \cos\left(\frac{1}{t}\right), \sqrt{4-t^2} \right\rangle$.

a.) (2 pts) What is the domain of $\mathbf{r}(t)$? Use interval notation.

b.) (6 pts) Find $\mathbf{r}'(t)$ and the domain of $\mathbf{r}'(t)$. Use interval notation.

21. Consider $f(x) = \begin{cases} ax^2 + x + 1 & \text{if } x \leq -1 \\ bx - 1 & \text{if } x > -1 \end{cases}$.

a.) (4 pts) Find the value of a and b that make $f(x)$ differentiable everywhere.

b.) (3 pts) For the value of a and b found above, find $f'(x)$.