

Name \_\_\_\_\_ ID \_\_\_\_\_

MATH 251

Quiz 2

Fall 2005

Sections 503

P. Yasskin

Total	/34
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All Work Out: (2 points each, includes 9 points extra credit)

Consider the parametric curve with position vector  $\vec{r} = \left(t, t^2, \frac{2}{3}t^3\right)$ .

Compute each of the following:

1. velocity

$$\vec{v} =$$

2. acceleration

$$\vec{a} =$$

3. jerk

$$\vec{j} =$$

4. length of velocity Simplify. (Note the quantity in the square root is a perfect square.)

$$|\vec{v}| =$$

5. speed

$$\frac{ds}{dt} =$$

6. arclength between the points  $(0,0,0)$  and  $\left(1,1,\frac{2}{3}\right)$

$$L =$$

7. unit tangent vector

$$\hat{T} =$$

8. cross product of velocity and acceleration

$$\vec{v} \times \vec{a} =$$

9. length of cross product of velocity and acceleration

$$|\vec{v} \times \vec{a}| =$$

10. unit binormal

$$\hat{B} =$$

11. unit principal normal

$$\hat{N} =$$

12. curvature

$$\kappa = \frac{|\vec{v} \times \vec{a}|}{|\vec{v}|^3} =$$

13. torsion

$$\tau = \frac{\vec{v} \times \vec{a} \cdot \vec{j}}{|\vec{v} \times \vec{a}|^2} =$$

14. tangential acceleration (use 2 methods)

$$a_T = \vec{a} \cdot \hat{T} =$$

15.  $a_T = \frac{d}{ds} \frac{ds}{dt} =$

16. normal acceleration (use 2 methods)

$$a_N = \vec{a} \cdot \hat{N} =$$

17.  $a_N = \kappa |\vec{v}|^2 =$