Name $\qquad$ Sec $\qquad$ MATH 251/253 Quiz $3 \quad$ Spring 2008
Section 508/200,501,502

| 1 | $/ 10$ | 3 | $/ 10$ |
| :---: | ---: | :---: | ---: |
| 2 | $/ 5$ | Total | $/ 25$ |

1. (10 points) Find all critical points of the function $f=2 x^{2} y+3 x y^{2}+6 x y$. Then use the $2^{\text {nd }}$ Derivative Test to classify each as a local minimum, local maximum or saddle point or say the test fails.
2. (5 points) If the temperature in a room is given by $T=75+x y+x z+y z$. Find the rate of change of the temperature in the direction of the vector $(12,4,3)$ at the point $(1,0,2)$.
3. (10 points) A rectangular box sits on the $x y$-plane with its upper vertices on the elliptic paraboloid $z=36-9 x^{2}-4 y^{2}$. Find the dimensions and volume of the largest such box.
