

MATH 152, Fall 2018

Worksheet 8

1. Does the series

$$\sum_{n=3}^{\infty} (-1)^n \frac{\sqrt{n}}{n-2}$$

converge absolutely or diverge?

2. For the next problem, show that the series converge to a some sum S , then find the smallest value of n so that the n -th partial sum s_n will guarantee the approximation of S to the required accuracy.

$$\sum_{k=1}^{\infty} \frac{(-1)^{k+1}}{\sqrt[4]{k+7}}; \quad |S - s_n| < 0.02$$

3. Use the Ratio Test to determine whether the series is convergent or divergent.

$$\sum_{n=1}^{\infty} \frac{\cos(n\pi/3)}{n!}$$

4. Use the Ratio Test to determine whether the series is convergent or divergent.

$$1 - \frac{2!}{1 \cdot 3} + \frac{3!}{1 \cdot 3 \cdot 5} - \frac{4!}{1 \cdot 3 \cdot 5 \cdot 7} + \cdots + (-1)^{n-1} \frac{n!}{1 \cdot 3 \cdot 5 \cdot \cdots \cdot (2n-1)}$$

5. A series $\sum_{n=1}^{\infty} a_n$ is defined by the equations

$$a_1 = 1; \quad a_{n+1} = \frac{2 + \cos n}{\sqrt{n}} a_n$$

Determine whether the series is convergent or divergent.

6. Does the series

$$\sum_{n=3}^{\infty} \frac{\sin(n\pi/6)}{1 + n\sqrt{n}}$$

converge absolutely, converge conditionally, or diverge?