

Week-in-Review

Exam 1 Review

1. $\int \frac{\cos^3(\ln x)}{x} dx$

2. The force required to hold a spring stretched to a length of 7 m is 5 N. Find the work required to stretch the spring from a length of 4 m to 8 m. The natural length of the spring is 3 m.

3. Find the volume of the solid S whose base is bounded by the region $x^2 + 4y^2 = 4$, and cross-sections perpendicular to the y -axis are isosceles triangles with height equal to the base.

4. Find the area bounded by $x = 3y - y^2$ and $y = -\frac{x}{2}$.

5. $\int \frac{\ln x}{\sqrt{x}} dx$

6. The region bounded by $y = \frac{1}{x^2}$, $x = 1$, $x = e$, and $y = 0$ is rotated around the y -axis. Find the volume.

7. The region bounded by $x + y^2 = 4$ and $x - y = 2$ is rotated around the line $x = -1$. Set up but do not evaluate an integral representing the volume of the solid.

8. $\int_0^2 x^2 e^{3x} dx$

9. Find the area bounded by $y = 7 - x^2$ and $y = 2x^2 - 5$.

10. Set up but do not evaluate an integral for the volume of the solid obtained by rotating the region bounded by $y = x^2 - x$ and $y = 2$ rotated around the line $x = 3$.

11.
$$\int \frac{x^3}{(x^2 + 1)^8} dx$$

12. Find the volume of the solid obtained by rotating the region bounded by $y = \sqrt{x}$, $y = 2$, and $x = 0$ around the y -axis.

13. $\int \tan^6 x \sec^4 x \, dx$

14. $\int_0^{\pi/6} \sin^2(5x) \, dx$

15. Find $\int e^x \sin(8x) dx$

16. A bucket attached to a 20 pound rope is used to draw water out of an 80 ft well. The bucket weighs 1 pound and holds 26 pounds of water. How much work is done in drawing up one full bucket of water?

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17. Consider the region R bounded by $y = x^3$, $y = 8$, and $x = 0$. Suppose a tank is in the shape of the region R revolved around the y -axis, and the units are measured in meters. If the tank is filled with water to a depth of 3 m, set up but do not evaluate an integral that gives the work done in pumping all the water out of a 1 m high spout. Use ρg for the weight density of water.