

Spring 2019 Math 152

Week in Review 5

courtesy: Amy Austin
(covering section 7.4, 7.8)

Section 7.4

1. $\int \frac{4x + 5}{2x^3 + 5x^2 + 3x} dx$
2. $\int \frac{x^3 + 2x + 1}{x^2 + 4x} dx$
3. $\int_1^2 \frac{dx}{x(x^2 + 2x + 1)}$
4. $\int \frac{3x^2 - 4x + 5}{(x - 1)(x^2 + 1)} dx$
5. $\int \frac{x + 6}{(x^2 + 1)(x^2 + 4)} dx$

Section 7.8

6. Determine whether the following improper integrals converge or diverge. If it converges, find the value of the integral. If it diverges, explain why.

a.) $\int_2^\infty \frac{x}{x^2 + 1} dx$

b.) $\int_e^\infty \frac{1}{x(\ln x)^4} dx$

c.) $\int_0^\infty xe^{-x} dx$

d.) $\int_{-\infty}^0 \frac{1}{1 - 2x} dx$

e.) $\int_{-\infty}^\infty \frac{dx}{x^2 + 9}$

f.) $\int_{-3}^0 \frac{dx}{(x + 3)^2}$

g.) $\int_0^3 \frac{1}{2x - 1} dx$

7. Determine whether the following integrals converge or diverge using the comparison theorem:

a.) $\int_0^\infty \frac{x - 1}{x^{10} + e^{5x}} dx$

b.) $\int_2^\infty \frac{x}{x^{3/2} - x - 1} dx$

c.) $\int_1^\infty \frac{\cos^2 x}{x^4} dx$

d.) $\int_1^\infty \frac{\sin(4x) + 9}{x^2 + x + 1} dx$