CHAPTER 16 – IDENTIFICATION NUMBERS

Consider the UPC code on a can of RO \star TEL tomatoes



The scanner is not working so the clerk enters the numbers by hand as

0 64144 28263 2

and this is invalid even though the product code for the mild version of this is 28263. What happened?

The UPC codes use a *check digit* to minimize scanning errors. A check digit is a digit included in a code to help detect errors.

For a UPC code $a_1a_2a_3a_4a_5a_6a_7a_8a_9a_{10}a_{11}a_{12}$ has a_{12} chosen so that the sum

$$3(a_1 + a_3 + a_5 + a_7 + a_9 + a_{11}) + 1(a_2 + a_4 + a_6 + a_8 + a_{10})$$

is evenly divisibly by 10. What is the check digit for the mild $RO \star TEL$?

06414428263

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The numbers 20, 60, and 100 are all evenly divisible by 10 so can we find a way to talk about numbers when we only care about the remainders?

Definition: Congruence Modulo m

Let *a*, *b*, and *m* be integers with $m \ge 2$. Then *a* is congruent to *b* modulo *m*, written

 $a \equiv b \mod m$

means that *m* evenly divides a-b.

Determine if the congruences below are true or false:

 $25 \equiv 1 \mod 6 \qquad \qquad 100 \equiv 20 \mod 10$

 $52 \equiv 0 \mod 13 \qquad \qquad 75 \equiv 7 \mod 5$

x mod *y* is equal to the remainder when you divide *x* by *y*.

Find the following values:

(a) $34 \mod 5 =$ _____

(b) 78 mod 11 = _____

(c) $13 \mod 15 =$ _____

(d) $12 \mod 2 =$

Types of errors when dealing with identification numbers:

- Replacing one digit with a different digit (single digit error)
 o ac entered rather than ab
- Transposing two adjacent digits (adjacent transposition error)
 ba entered rather than *ab*
- Transposing a sequence of digits (jump transposition error)
 cba entered rather than *abc*

Note that some of the digits in the UPC code are multiplied by 3. Those digits had a *weight* of 3.

A code $a_1a_2a_3a_4a_5a_6$ uses the last digit as a check digit. The check digit is found using the formula

 $a_6 = a_1 + a_3 + 3(a_2 + a_4) \mod 10$

(a) What is the check digit for the code 23714?

(b) Find the value of the missing digit x in the code 46x782

(c) Will this code find an error if the first digit is entered incorrectly?

A code is given by $a_1a_2a_3$ where a_3 is the check digit and $a_3 = a_1 + 4 a_2 \mod 9$ (a) Will this check digit find all transposition errors?

(b) Will this check digit find all single digit errors in the first position?

(c) Will this check digit find all single digit errors in the second position?

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Data can be encoded in identification numbers.

The last 5 digits of Illinois driver's license numbers are based on the driver's birthday and gender. For a man, the last 5 digits are the birth year followed by the day of the year based on each month having 31 days. For a woman, 600 is added to the number.

(a) What would the last 5 digits of an of Illinois driver's license number look like for a man born on February 12, 1967?

(b) What do you know about a person who has the last 5 digits 10642?

(c) What do you know about a person who has the last 5 digits 90373?

SAMPLE EXAM QUESTIONS FROM CHAPTER 16

1. Determine the check digit that should be appended to the identification number 634498, if the check digit is the number needed to bring the total of all the digits to a multiple of 10.

(A) The code is invalid(B) 6(C) 8(D) 4(E) None of these

2. Which, if any, of the statements below are true? Mark all correct answers.

- (A) $101 \equiv 1 \mod 2$
- (B) $77 \equiv 0 \mod 11$
- (C) $49 \equiv 1 \mod 12$

(D) $39 \equiv 5 \mod 5$

(E) None of these are true.

3. The number 4320 is accidentally entered as 4321. What type of error is this?

- (A) A transposition error
- (B) A jump transposition error
- (C) A single digit error
- (D) A baseball error
- (E) None of these

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4. The last three digits of a man's ID number are the birth day of the year based on each month of the year having 35 days. If the person is a woman, 500 is added to the birth day.

(a) What are the last three digits of a man's ID number if he was born on October 8th?

(b) What do you know about a person if the last three digits of the person's ID number are 503?

(c) What do you know about a person if the last three digits of the person's ID number is 420?

5. A code is given by $a_1a_2a_3a_4$ where a_4 is the check digit. The check digit is $a_4 = 7a_1 + 2a_2 + 5a_3 \mod 9$.

(a) Determine the value of x in the code 2x45, given that the check digit is valid.

(b) Determine if the check digit will find all single digit errors in the third position.

(c) Determine if the check digit will find all transposition errors in the second and third positions.