# Chapter 2: Systems of Linear Equations and Matrices

### 2.1 Systems of Linear Equations: An Introduction

1. The two lines intersect.



2. The two lines are the same.





\_\_\_\_\_×

This system is called dependent.

The solution is a parametric solution (infinite).

We can consider *y* as a parameter,

Particular solutions:



#### Example: Three Linear Equations with 3 Variables



NO SOLUTION

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**Formulating Linear Systems** 

An apartment complex is being developed that has small, large, and luxury apartments. The developer has decided that there will be a total of 192 apartments. The number of bigger apartments (large and luxury) will equal the number of small apartments. The number of small apartments will be three times the number of luxury apartments. How many apartments of

Zelda has \$8,900 to invest. She decides to invest all of her money in three different funds. The PX Company costs \$50 per share and pays dividends of \$1.00 per share each year. The NY Company costs \$90 per share and pays dividends of \$2.00 per share each year. The LZ Company costs \$40 per share and pays dividends of \$1.60 per share per year. Zelda wants to invest half as much money in the LZ Company as in the NY Company and wants to earn \$222 in dividends per year. How many shares of each company should Zelda buy to meet her goal?

v	_	
A	_	
		_

y = \_\_\_\_\_

*z* = \_\_\_\_\_

"The PX Company costs \$50 per share and pays dividends of \$1.00 per share each year." If you buy x shares in the PX Company,

How much does it cost? \$\_\_\_\_ How much do you earn in dividends? \$\_\_\_\_\_

"The NY Company costs \$90 per share and pays dividends of \$2.00 per share each year." If you buy *y* shares in the NY Company,

How much does it cost? \$\_\_\_\_ How much do you earn in dividends? \$\_\_\_\_\_

"The LZ Company costs \$40 per share and pays \$1.60 per share per year in dividends." If you buy *z* shares in the LZ Company,

How much does it cost? \$\_\_\_\_ How much do you earn in dividends? \$\_\_\_\_\_ Write an equation for the statement "Zelda has \$8,900 to invest."

Write an equation for the statement "Zelda wants to earn \$222 in dividends per year."

"Zelda wants to invest half as much money in the LZ Company as in the NY Company."

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#### 2.2 Systems of Linear Equations: Unique Solutions

You may:

- Interchange any two of the equations.
- Multiply an equation by a non-zero constant.
- Add a multiple of one equation to another.

2x - y = 6x + 2y = -2

# AUGMENTED MATRIX form

Rules are

- Interchange any of the rows equations.
- Multiply a row by a non-zero constant.
- Add a multiple of one row to another.

## What is RREF form?

- 1. All rows consisting entirely of zeros are at the bottom of the matrix
- 2. The first non-zero entry in any row is a 1 (called a leading 1)
- 3. In any two successive non-zero rows the leading 1 in the lower row lies to the right of the leading 1 in the upper row.
- 4. If a column contains a leading 1, then the rest of the entries in that column are 0's.

*PIVOT* on an element – make the element a 1 and the rest of the entries in that column 0's.

Gauss-Jordan Method – Pivot until the augmented matrix is in RREF form.

x + y + z = 192y + z = xx = 3z

2x - y = 6x + 2y = -2

The goal is to get the augmented matrix into row-reduced echelon form (RREF).

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