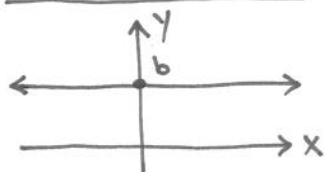
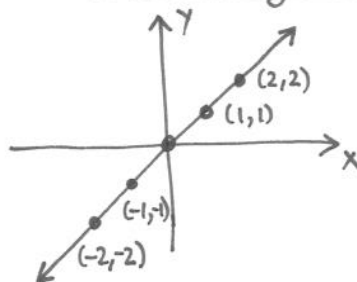


Library of Functions

① Constant Function : $f(x) = b$

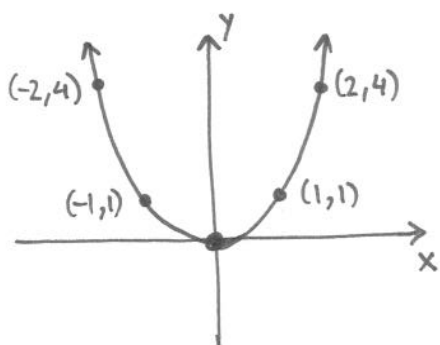


② Identity Function : $f(x) = x$



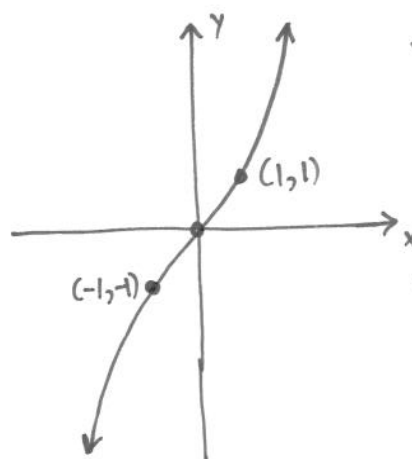
Domain: $(-\infty, \infty)$
 Range: $(-\infty, \infty)$
 Intercepts: $(0, 0)$
 Symmetry: origin
 (odd function)

③ Square Function : $f(x) = x^2$



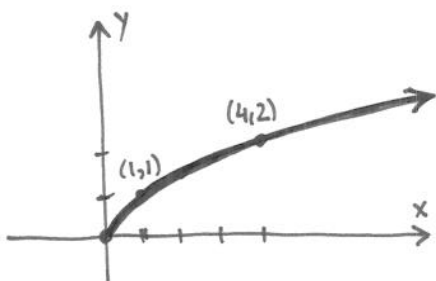
Domain: $(-\infty, \infty)$
 Range: $[0, \infty)$
 Intercepts: $(0, 0)$
 Symmetry: y-axis
 (even function)

④ Cube Function : $f(x) = x^3$



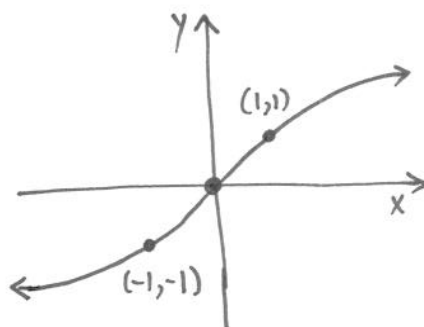
Domain: $(-\infty, \infty)$
 Range: $(-\infty, \infty)$
 Intercepts: $(0, 0)$
 Symmetry: origin
 (odd function)

⑤ Square Root Function : $f(x) = \sqrt{x}$



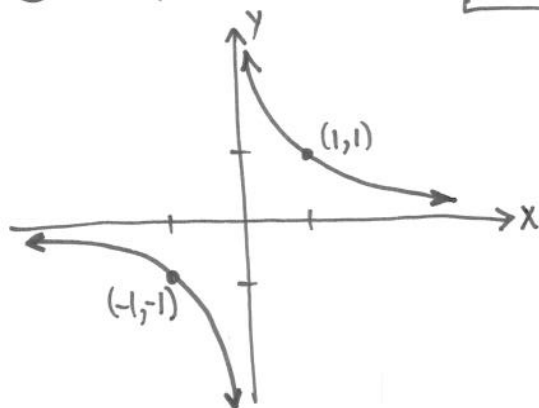
Domain: $[0, \infty)$
 Range: $[0, \infty)$
 Intercepts: $(0, 0)$
 Symmetry: none

⑥ Cube Root Function : $f(x) = \sqrt[3]{x}$



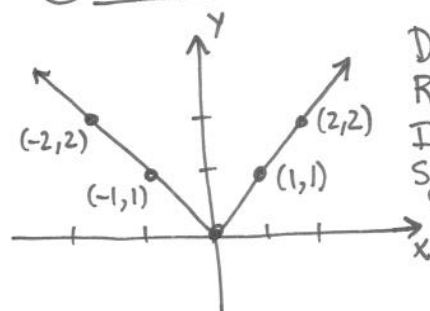
Domain: $(-\infty, \infty)$
 Range: $(-\infty, \infty)$
 Intercepts: $(0, 0)$
 Symmetry: origin
 (odd function)

⑦ Reciprocal Function : $f(x) = \frac{1}{x}$



Domain: $(-\infty, 0) \cup (0, \infty)$
 Range: $(-\infty, 0) \cup (0, \infty)$
 Intercepts: none
 Symmetry: origin
 (odd function)

⑧ Absolute Value Function : $f(x) = |x|$



Domain: $(-\infty, \infty)$
 Range: $[0, \infty)$
 Intercepts: $(0, 0)$
 Symmetry: y-axis
 (even function)

Graphing Transformations

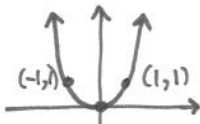
To Graph:

Graph $f(x)$ and:

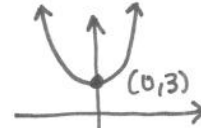
Examples:

$y = f(x) + k$

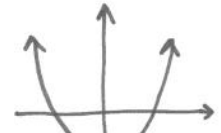
Shift \uparrow k units



Basic function x^2



$x^2 + 3$



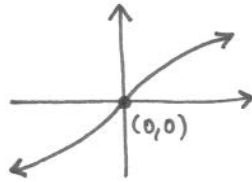
$x^2 - 3$

$y = f(x) - k$

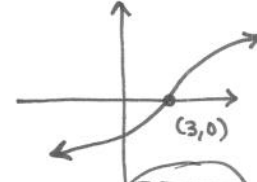
Shift \downarrow k units

$y = f(x+k)$

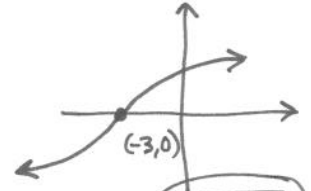
Shift \leftarrow k units



Basic function $\sqrt[3]{x}$



$\sqrt[3]{x-3}$



$\sqrt[3]{x+3}$

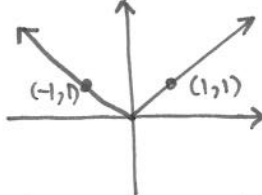
$y = f(x-k)$

Shift \rightarrow k units

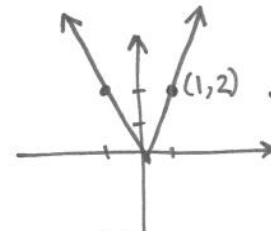
$y = a f(x)$

If $0 < a < 1$, vertically compress

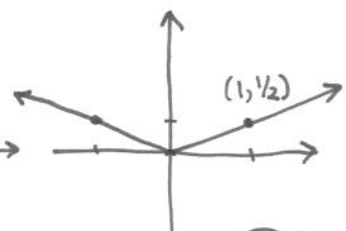
If $a > 1$, vertically stretch



Basic function $|x|$



$2|x|$

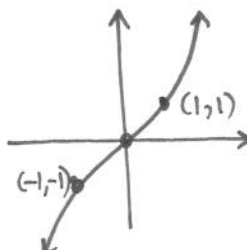


$\frac{1}{2}|x|$

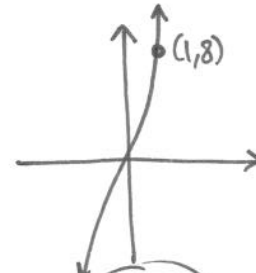
$y = f(ax)$

If $a > 1$, horizontally compress

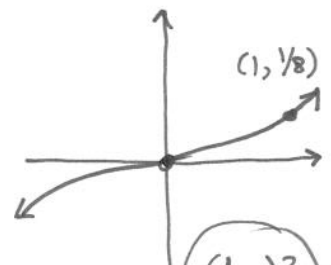
If $0 < a < 1$, horizontally stretch



Basic function x^3



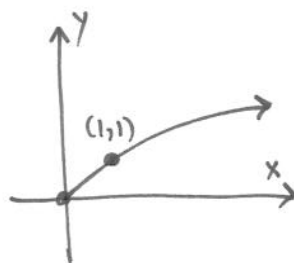
$(2x)^3$



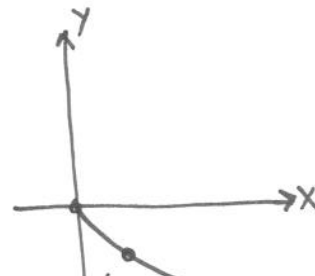
$(\frac{1}{2}x)^3$

$y = f(-x)$

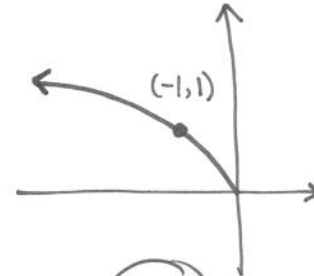
Reflect about the y -axis



Basic function \sqrt{x}



$-\sqrt{x}$



$\sqrt{-x}$

$y = -f(x)$

Reflect about the x -axis