

Name: _____

March 23rd, 2015.
Math 2401; Sections K1, K2, K3.
Georgia Institute of Technology
Exam 3

I commit to uphold the ideals of honor and integrity by refusing to betray the trust bestowed upon me as a member of the Georgia Tech community. By signing my name below I pledge that I have neither given nor received help on this exam.

Pledged: _____

| Problem | Possible Score | Earned Score |
|---------|----------------|--------------|
| 1 | 20 | |
| 2 | 20 | |
| 3 | 20 | |
| 4 | 18 | |
| 5 | 16 | |
| 6 | 6 | |
| Total | 100 | |

Remember that you must SHOW YOUR WORK to receive credit!

Good luck!

2. [20 points] Find:

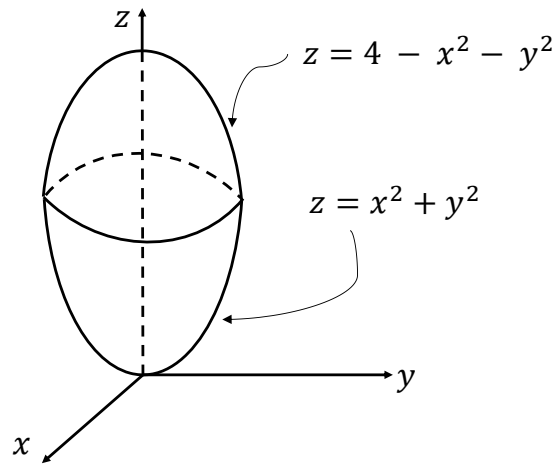
$$\int_1^2 \int_1^{\sqrt{z}} \int_{\ln(x)}^{\ln(3x)} e^{x^2+y+z} dy dx dz.$$

5. [16 points] Using *cylindrical coordinates*, set up the triple integral to compute the volume of the solid enclosed by the two paraboloids:

$$z = 4 - x^2 - y^2;$$

$$z = x^2 + y^2,$$

pictured below. You do not have to compute the value of the integral.



Name: _____

April 15th, 2015.
Math 2401; Sections K1, K2, K3.
Georgia Institute of Technology
Exam 4

I commit to uphold the ideals of honor and integrity by refusing to betray the trust bestowed upon me as a member of the Georgia Tech community. By signing my name below I pledge that I have neither given nor received help on this exam.

Pledged: _____

| Problem | Possible Score | Earned Score |
|---------|----------------|--------------|
| 0 | 10 | 10 |
| 1 | 18 | |
| 2 | 18 | |
| 3 | 18 | |
| 4 | 18 | |
| 5 | 18 | |
| Total | 100 | |

Remember that you must SHOW YOUR WORK to receive credit!

Good luck!

1. [18 points] Find the line integral:

$$\int_C 3x \, ds,$$

where C is the portion of the parabola $y = x^2$ from $(0, 0)$ to $(3, 9)$.

2. [18 points] Find:

$$\oint_C (y + e^{\sqrt{x}}) dx + (2x + \cos y^2) dy,$$

where C is the positively oriented boundary of the region enclosed by the parabolas $y = x^2$ and $x = y^2$.

3. [18 points] Consider the conservative field:

$$\mathbf{F}(x, y, z) = (yz)\mathbf{i} + (xz - 2y \ln(z))\mathbf{j} + \left(xy - \frac{y^2}{z}\right)\mathbf{k}.$$

- a). [12 points] Find a potential function for this field.
b). [6 points] Find $\int_C \mathbf{F} \cdot d\mathbf{r}$, where C is the curve:

$$\mathbf{r}(t) = \langle t, t^2, e^t \rangle, \quad 0 \leq t \leq 1.$$

5. [18 points] Compute the area enclosed by the deltoid curve, pictured below, and parametrized by:

$$\mathbf{r}(\theta) = \langle 2 \cos \theta + \cos(2\theta), 2 \sin \theta - \sin(2\theta) \rangle, \quad 0 \leq \theta \leq 2\pi.$$

Reminders: $\sin(2\theta) = 2 \sin \theta \cos \theta$ and $\cos(2\theta) = \cos^2 \theta - \sin^2 \theta = 2 \cos^2 \theta - 1 = 1 - 2 \sin^2 \theta$.

