

Section 10.1: Curves Defined by Parametric Equations

Example: Use the parametric function  $x(t) = t^2 + 3t$ ,  $y(t) = 2t + 5$  to answer the following.

A) Is the point (10,8) on the graph? Justify your answer.

No.

$$2t + 5 = 8$$

$$2t = 3$$

$$t = 3/2$$

$$x(3/2) = (3/2)^2 + 3(3/2)$$

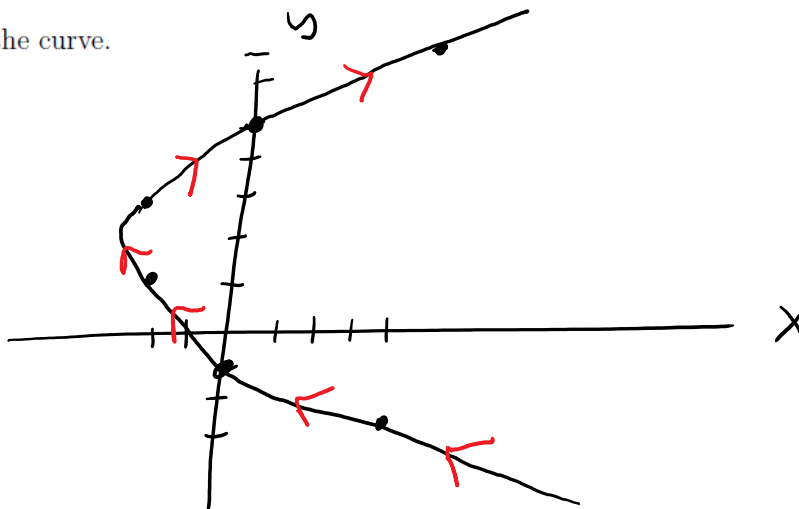
$$= 9/4 + 9/2$$

$$= 9/4 + 18/4$$

$$= 27/4 \neq 10$$

B) Sketch the graph of the curve.

t	x	y
-4	4	-3
-3	0	-1
-2	-2	1
-1	-2	3
0	0	5
1	4	7
2	10	9



C) Find the Cartesian equation of the parametric function.

$$x = t^2 + 3t$$

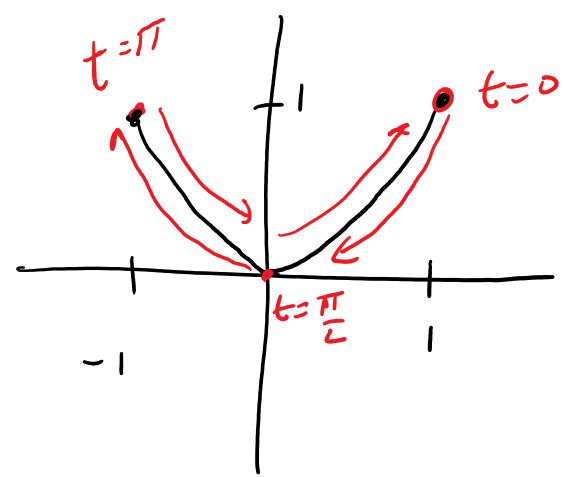
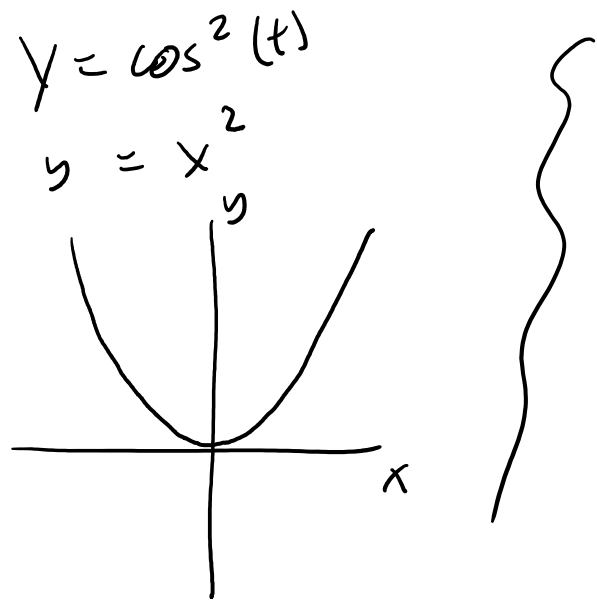
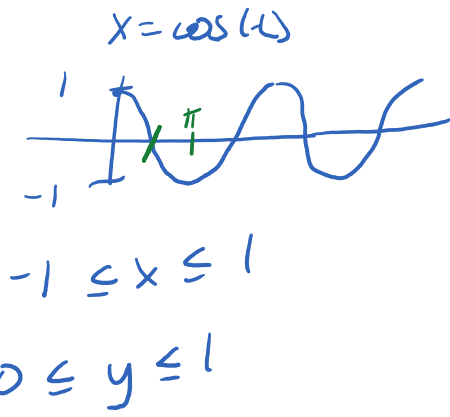
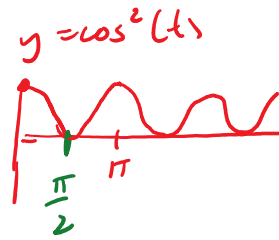
$$y = 2t + 5$$

$$y - 5 = 2t$$

$$\frac{y - 5}{2} = t$$

$$x = \left(\frac{y-5}{2}\right)^2 + 3\left(\frac{y-5}{2}\right)$$

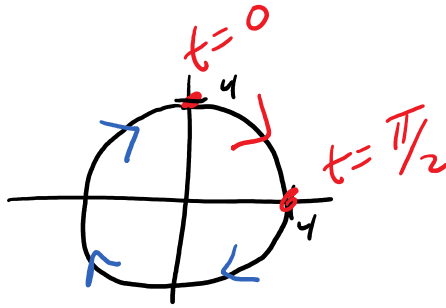
Example: Sketch the curve  $x = \cos(t)$ ,  $y = \cos^2(t)$ .



Example: Sketch the graph of these parametric curves.

A)  $x = 4 \sin(t)$ ,  $y = 4 \cos(t)$

$$\frac{x}{4} = \sin(t) \quad \frac{y}{4} = \cos(t)$$



$$\begin{aligned} \sin^2 t + \cos^2 t &= 1 \\ \left(\frac{x}{4}\right)^2 + \left(\frac{y}{4}\right)^2 &= 1 \\ \frac{x^2}{16} + \frac{y^2}{16} &= 1 \\ x^2 + y^2 &= 16 \end{aligned}$$

B)  $x = 4 \cos(t)$ ,  $y = 4 \sin(t)$

