## Appendix J.1: Vectors

**Definition:** A vector is a quantity that has both a magnitude and a direction. A two-dimensional vector is an ordered pair  $\mathbf{a} = \langle a_1, a_2 \rangle$  of real numbers. The numbers  $a_1$  and  $a_2$  are called the components of  $\mathbf{a}$ .

Example: Graph the vector  $\langle 3, 4 \rangle$ .



Example: For the points, A(1, -2) and B(5, 4), find  $\overrightarrow{AB}$  and  $\overrightarrow{BA}$ .

**Definition:** Given two points  $J(a_1, a_2)$  and  $K(b_1, b_2)$ , then the vector represended by  $\overrightarrow{JK} =$ 

**Definition:** The **magnitude** or **length** of a vector  $\mathbf{a} = \langle a_1, a_2 \rangle$  is

## $|\mathbf{a}| =$

Example: Find the length of these vectors.

A)  $\langle 4,6\rangle$ 

B)  $\langle 0, 0 \rangle$ 

Scalar Multiplication: If c is a scalar and  $\mathbf{a} = \langle a_1, a_2 \rangle$ , then we define the vector  $c\mathbf{a}$  as  $c\mathbf{a} =$ 

 $|c\mathbf{a}| =$ 

**Definition:** Two vectors, **a** and **b** are said to be **parallel** if there is some scalar c such that  $\mathbf{a} = c\mathbf{b}$ 

Vector Addition/Subtraction: If  $\mathbf{a} = \langle a_1, a_2 \rangle$  and  $\mathbf{b} = \langle b_1, b_2 \rangle$  then the vector  $\mathbf{a} + \mathbf{b}$  and  $\mathbf{a} - \mathbf{b}$  are defined as

 $\mathbf{a} + \mathbf{b} =$ 

 $\mathbf{a} - \mathbf{b} =$ 

Example: Compute the following for  $\mathbf{a} = \langle 3, 4 \rangle$ ,  $\mathbf{b} = \langle 6, 2 \rangle$ ,  $\mathbf{c} = \langle -2, 5 \rangle$ 

A)  $\mathbf{a} + \mathbf{b}$ 

B)  $2\mathbf{a} + 3\mathbf{b}$ 

D)  $3\mathbf{a} - 2\mathbf{c} + \mathbf{b}$ 

**Definition:** A unit vector is a vector of length 1. The vectors  $\mathbf{i} = \langle 1, 0 \rangle$  and  $\mathbf{j} = \langle 0, 1 \rangle$  are referred to as the standard basis vectors for the xy plane.

Example: Find a vector of length 7 that is in the same direction as  $\mathbf{a} = \langle 3, 4 \rangle$ 

Example: Given the points P(1,5) and Q(3,10). Find a vector of length 4 that is in the same direction as  $\overrightarrow{QP}$ .

Example: A pilot is flying in the direction of  $N60^{o}W$  at a speed of 250km/hr.

A) Find the velocity vector.

B) If there is a wind blowing in the direction of N45 $^{o}$ E at 30km/hr, find the true course and ground speed of the plane.

Example: A 50lb weight hangs from 2 wires. Find the tensions (forces)  $T_1$  and  $T_2$  in both wires and their magnitudes.

