Section 6.1: Area between Curves

Consider the continuous functions f(x) and g(x) with the property on the interval [a, b] that both are above the x-axis and $f(x) \ge g(x)$. Write down the computation that will give the area bounded between these functions on this interval.



For the next graphs, set-up the integral(s) that will give the area that is bounded between f(x) and g(x) on the interval [a, b].





Example: Find the area that is bounded by these curves.

y = x + 3 $y = x^2 - 9$

Example: Find the area that is bounded by these curves.

 $\begin{aligned} x &= y^2 \\ x &= 2y^2 - 4 \end{aligned}$

 $y = e^{-3x}$ $y = e^x$

Example: Set up the integral(s), with respect to the variable y, that gives the area that is bounded(enclosed) by these curves.

 $y = 2\sqrt{x}$ $y = \frac{-x}{3}$

3x + y = 16

Example: Set up the integral(s) that will give area that is bounded by these curves on the interval $-2 \le y \le 3$.

 $\begin{aligned} x &= y^2 - 4y \\ y &= 0.5x \end{aligned}$

Example: Set up the integral(s) that will give area that is bounded by these curves from x = 0 to $x = 2\pi$.

 $y = \sin(x)$ $y = 2 - 3\sin(x)$

Example: Set up the integral(s) that will give area that is bounded by these curves x = |y - 1| and $x = y^2 - 3$ with the condition that $y \ge 0$