

Final Exam Information

You are encouraged to check this document to make sure that I did not accidentally have typos in any of the formulas.

Chapter 7

- Cash flows (in and out)
- net present value, $P(i)$, of a set of cash flows
- IRR, internal rate of return, also called the yield rate.
- computation

by formula

can be difficult depending on the number of cash flows.

BA calc

CF, NPV, and IRR buttons.

TI-84

$\text{npv}(\text{rate}, \text{initial}, \{\text{cash flow}\}, \{\text{cash flow freq.}\})$
 $\text{irr}(\text{initial}, \{\text{cash flow}\}, \{\text{cash flow freq.}\})$

- Yield rate unique
calculator tend to give the one closest to zero if not unique.
- Reinvesting dividends/mortgage payments/bond payments at a different rate than the original account.

need to know formulas from the second exam material.

FV of a set of payments

FV of a set of increasing payments

Bond pricing and calculations

overall yield of the investment(adjusted yield rate).

- Interest measurement of a fund
A= amount at beginning of the period
B= amount at the end of the period
I= amount of interest earned during the period
C= total net amount of the principal contributed during the period.

Yield of the fund.

Actual yield, IRR

computed with formulas or cash flow worksheet

Simple interest approximation to IRR

$$IRR \approx i^{DW} = \frac{I}{A + \sum C_t(1-t)}$$

approximation to the dollar weighted approximation of the yield. can be used when there are lots of cash flows during the period or when just given overall totals.

$$i^{DW} \approx \frac{I}{A + \frac{1}{2}C} = \frac{2I}{A + B - I}$$

Time-weighted rate of interest, i^{TW}

$$1+i^{TW} = \left(\frac{B_1}{B_0}\right) \left(\frac{B_2}{B_1 + C_1}\right) \cdots \left(\frac{B_m}{B_{m-1} + C_{m-1}}\right)$$

- Portfolio Method for investment funds
- Investment Year method for investment funds

Chapter 10

- Yield Curve
- Spot Rates

Finding PV of a bond/investment

Computing from zero coupon bonds.

computing with bootstrap method using coupon bonds

at-par-yield rate

- Forward Rates
single year
multi-year
- relationship between spot rates and forward rates.
- computing forward rates from different investments.

Chapter 11

$$\bullet NPV = P(i) = \sum_{t=1}^n R_t v^t = \sum_{t=1}^n R_t (1+i)^{-t}$$

$$P'(i) = \sum_{t=1}^n -t R_t v^{t+1} = \sum_{t=1}^n -t R_t (1+i)^{-t-1}$$

$$P''(i) = \sum_{t=1}^n t(t+1) R_t v^{t+2} = \sum_{t=1}^n t(t+1) R_t (1+i)^{-t-2}$$

- Duration

Macaulay duration(Mac d)

$$\bar{d} = \frac{\sum_{t=1}^n t * v^t R_t}{PV}$$

for equal payments of R

$$\bar{d} = \frac{R(Ia)_{\overline{n}|}}{Ra_{\overline{n}|}}$$

$$(Ia)_{\overline{n}|} = \frac{\ddot{a}_{\overline{n}|} - nv^n}{i} = a_{\overline{n}|} + \frac{a_{\overline{n}|} - nv^n}{i}$$

$$(Ia)_{\infty|} = \frac{1}{i} + \frac{1}{i^2}$$

for a single payment

\bar{d} =time of the payment

Modified duration(Mod d)

$$\bar{v} = \frac{-P'(i)}{P(i)}$$

$$\bar{d} = (1 + i)\bar{v}$$

- Using a first degree taylor polynomial to approximate the price when there is a small change in the interest rate.

$$P(i + h) \approx P(i) + P'(i)H = P(i)[1 - \bar{v}h]$$

- Convexity

$$\bar{c} = \frac{P''(i)}{P(i)}$$

- Using a second degree taylor polynomial to approximate the price when there is a small change in the interest rate.

$$P(i + h) \approx P(i) + P'(i)h + P''(i)\frac{h^2}{2}$$

$$= P(i)[1 - \bar{v}h + \bar{c}\frac{h^2}{2}]$$

- $\frac{d}{di}\bar{v} = \bar{v}^2 - \bar{c}$

- multiple securities: P_1, \dots, P_m

$$\bar{d} = \frac{\bar{d}_1 P_1 + \bar{d}_2 P_2 + \dots + \bar{d}_m P_m}{P}$$

$$\bar{v} = \frac{\bar{v}_1 P_1 + \bar{v}_2 P_2 + \dots + \bar{v}_m P_m}{P}$$

$$\bar{c} = \frac{\bar{c}_1 P_1 + \bar{c}_2 P_2 + \dots + \bar{c}_m P_m}{P}$$

- Analyzing a portfolio with multiple interest rate.

- Absolute Matching/Dedication method to match cash outflows with cash inflows.
- Redding Immunization
- Full Immunization

Any additional topic/information covered in these chapters.