

## BASIC DIFFERENTIATION FORMULAS

$$(c)' = 0$$

$$(x^n)' = nx^{n-1}$$

$$(a^x)' = a^x \ln a, \text{ in particular } (e^x)' = e^x$$

$$(\log_a x)' = \frac{1}{x \ln a}, \text{ in particular } (\ln x)' = \frac{1}{x}$$

$$(\sin x)' = \cos x$$

$$(\cos x)' = -\sin x$$

$$(\tan x)' = \sec^2 x = \frac{1}{\cos^2 x}$$

$$(\cot x)' = -\csc^2 x = -\frac{1}{\sin^2 x}$$

$$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$$

$$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$$

$$(\arctan x)' = \frac{1}{1+x^2}$$

$$(\operatorname{arccot} x)' = -\frac{1}{1+x^2}$$

### Properties of derivatives:

$$(u \pm v)' = u' \pm v'$$

$$(cu)' = cu'$$

$$(uv)' = u'v + uv'$$

$$\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2}$$

$$(f(u(x)))' = f'(u)u'(x) \text{ (the chain rule)}$$

Here  $\arcsin x = \sin^{-1} x$ ,  $\arccos x = \cos^{-1} x$ ,  $\arctan x = \tan^{-1} x$ , and  $\operatorname{arccot} x = \cot^{-1} x$

## BASIC INTEGRATION FORMULAS

$$\int dx = x + c$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + c \quad (n \neq -1)$$

$$\int \frac{dx}{x} = \ln |x| + c$$

$$\int a^x dx = \frac{a^x}{\ln a} + c, \text{ in particular}$$

$$\int e^x dx = e^x + c$$

$$\int \sin x dx = -\cos x + c$$

$$\int \cos x dx = \sin x + c$$

$$\int \sec^2 x dx = \tan x + c$$

$$\int \csc^2 x dx = -\cot x + c$$

$$\int \frac{dx}{\sqrt{a^2-x^2}} = \arcsin \frac{x}{a} + c$$

$$\int \frac{dx}{\sqrt{x^2 \pm a^2}} = \ln |x + \sqrt{x^2 \pm a^2}| + c$$

$$\int \frac{dx}{a^2+x^2} = \frac{1}{a} \arctan \frac{x}{a} + c$$

$$\int cf(x)dx = c \int f(x)dx$$

$$\int (f(x) + g(x))dx = \int f(x)dx + \int g(x)dx$$

### Substitution:

if  $\int f(x)dx = F(x) + c$ , then

$$\int f(u(x))u'(x)dx = F(u(x)) + c$$

### Integration by parts:

$$\int uv'dx = uv - \int u'vdx$$

$$\text{or } \int u dv = uv - \int v du$$