## Answers to the sample problems for Test 2

1. (a) The exact cost of producing the 31st umbrella is $\$ 2 . C^{\prime}(31)=2$.
(b) The marginal revenue $R^{\prime}(x)=25-0.02 x$, the marginal average revenue $\bar{R}^{\prime}(x)=$ -0.01 .
(c) The average profit per umbrella if 20 umbrellas is produced is $\bar{P}(20)=-427.2$. The marginal average profit at a production level of 20 umbrellas is $\bar{P}^{\prime}(20)=22.49$. The average profit per umbrella if 21 umbrella is produced is $\bar{P}(20)+\bar{P}^{\prime}(20)=-404.71$.
2. (a) $\$ 15143.71$
(b) 14 years
3. $\$ 15163.27$
4. $8.66 \%$
5. 71 years
6. $y=3 x-3+\ln 2$.
7. $x=2$
8. (a) $\frac{1}{4} \frac{12 x^{2}+5}{\left(4 x^{3}+5 x+7\right) \ln 3}$.
(b) $-6 x^{2} 8^{1-2 x^{3}} \ln 8$
(c) $\frac{6 x\left(5-2 x^{2}\right)}{\left(x^{2}+5\right)^{4}}$
(d) $\left(2 x^{2}+4 x-5\right) e^{2 x+3}$
9. (a) $E(p)=\frac{p}{60-p}$.
(b) $30<p<60$
(c) the demand will increase by $1 \%$
(d) the revenue will increase
10. (a) $f^{\prime \prime}(x)=x\left(2 x^{3}-5\right)^{4}+144 x^{3}\left(2 x^{3}-5\right)^{3}+432 x^{6}\left(2 x^{3}-5\right)^{2}$
(b) $f^{\prime \prime}(x)=\frac{4}{x^{3}}-\frac{72}{x^{5}}$
11. (a) $(b, c) \cup(f, \infty)$
(b) $(a, b) \cup(c, f)$
(c) $b, f$
(d) $(a, c) \cup(c, d) \cup(e, g)$
(e) $(d, e) \cup(g, \infty)$
(f) $d, e, g$
12. (a) $x=\sqrt[3]{4} \approx 1.59$
(b) $f$ is increasing on $(1.59, \infty), f$ is decreasing on $(-\infty, 1.59)$
(c) $f$ has a local minimum at $(1.59,-4.76)$
(d) $f$ is concave upward on $(-\infty, \infty)$
(e) there are no inflection points.
13. The absolute maximum value for $f$ is 3 ; the absolute minimum value for $f$ is $\sqrt{5} \approx 2.236$.
14. The absolute minimum value for $f$ is -1 ; no absolute maximum.
15. $40 \mathrm{~cm} \times 40 \mathrm{~cm} \times 20 \mathrm{~cm}$
