

1. Find the domain of the function

$$f(x) = \begin{cases} x + 4, & \text{if } x > 3 \\ \frac{x}{\sqrt{x+2}}, & \text{if } x \leq 3 \end{cases}$$

2. Which of the following are polynomials? For each polynomial determine its degree and circle its leading coefficient.

(a) $f(x) = x^5 + x^2 - 6 - x^{11}$

(b) $g(x) = 5\sqrt{x} + 4x - 2$

(c) $h(x) = 2x^4 - x^2 + x$

(d) $r(x) = x^2 + x^{-2}$

3. Solve for x

$$7^{x^2} = 7^{2x+3}$$

4. Amanda would like to remodel her kitchen in 4 years. How much should she invest now at 7% compounded monthly to have \$15,000 four years from now? Round your answer to the nearest cent.

5. Solve for x

$$\log_5 x + \log_5(x + 3) = \log_5 10$$

6. Write as a single logarithm

7. The financial department of a company that produces pens obtains the following price-demand equation

$$p = 35 - 0.34x$$

where p is the wholesale price in dollars per pen at which x pens are sold. The fixed costs for the company is \$200 and the variable costs is \$4.50 per pen. How many pens should be produced by the company to maximize the profit? Round the answer to the nearest integer.

8. A company that produces and sells T-shirts established the price-demand function $p(x) = 21 - 0.1x$, where $p(x)$ is the price per T-shirt at which x T-shirts can be sold. Suppose that the company must produce at least 50 shirts and its cost equation is $C(x) = 2x + 250$. How many T-shirts must the company produce to break-even? Round your answer to the nearest T-shirt.
9. The quantity demanded of a certain brand of computers is 300/wk when unit price is \$450. For each decrease in unit price of \$30, the quantity demanded increases by 100 units. The company will not supply any computers if the unit price is \$250 or lower. However, they will supply 375 computers if unit price is \$325. Find the equilibrium price and the equilibrium quantity.

10. Suppose \$29,000 is deposited into an account paying 7.5% annual interest. How much will be in the account after 5 years if the account is compounded continuously?

11. Express the given quantities as a single logarithm:

(a) $\log_2 x + 5\log_2(x + 1) + \frac{1}{2}\log_2(x - 1)$

(b) $2\ln 4 - \ln 2$

12. How long will it take for the amount in an account to triple if the money is compounded continuously at an annual interest rate of 4.7%?

13. Evaluate the limit

(a) $\lim_{x \rightarrow 5} \frac{x^2 - 25}{x^2 + x - 30}$

(b) $\lim_{h \rightarrow 0} \frac{\sqrt{a+h} - \sqrt{a}}{h}, a \geq 0.$

(c) $\lim_{x \rightarrow \infty} \frac{2x^3 + 1}{4 - x - x^3}$

14. Find the vertical and horizontal asymptotes of the curve $y = \frac{x^2 + 4}{3x^2 - 3}$.

15. Find all points of discontinuity for the function

$$f(x) = \begin{cases} x^2 + 1 & , \text{ if } x < 2, \\ x + 2 & , \text{ if } x \geq 2. \end{cases}$$

16. The displacement of an object moving in a straight line is given by $s(t) = 1 + 2t + t^2/4$ (t is in seconds).

(a) Find the average velocity when t changes from $t = 1$ to $t = 2$.

(b) Find the velocity of the object when $t = 1$.

17. Find the equation of the tangent line to the curve $y = 2x^2 - 3$ at the point (2,5).