

Due Friday, Oct. 10, 2014 at the beginning of class

NAME (print): key**Instructions:**

- For problems 1 – 3 mark only one choice. Wrong answer will receive no credit. Each problem is worth 2 points.
- For Problem 4 present your solutions in the space provided. **Show all your work** neatly and concisely and **clearly indicate your final answer**. You will be graded not merely on the final answer, but also on the quality and correctness of the work leading to it. Credit will not be given for an answer not supported by work.
- STAPLE ALL THE SHEETS.

1. Given the cost function  $C(x) = x^3 - 10x^2 + 23x + 12000$ . Use the marginal cost function to approximate the cost of producing the 21st item.

(a) \$823

(b) \$17334

(c) \$16460

(d) \$926

(e) None of these

$$C'(x) = 3x^2 - 20x + 23$$

$$C'(20) = 3(20)^2 - 20(20) + 23 = \boxed{823}$$

2. Find the derivative of the function  $f(x) = (x^2 + x + 1)(x^2 + 2)$ .

(a)  $x^3 + 4x^2 + 3x + 2$

(b)  $4x^2 + 2x^2 + 1$

(c)  $4x^2 + 2x$

(d)  $4x^3 + 3x^2 + 6x + 2$

(e) None of these

$$\begin{aligned}
 f'(x) &= (2x+1)(x^2+2) + (2x)(x^2+x+1) \\
 &= 2x^3 + 4x + x^2 + 2 + 2x^3 + 2x^2 + 2x \\
 &= \boxed{4x^3 + 3x^2 + 6x + 2}
 \end{aligned}$$

3. Find an equation of the tangent line to the curve  $y = \frac{x}{x+3}$  at the point (6, 2).

(a)  $y = x + 8$

(b)  $y = -\frac{1}{3}x + 4$

(c)  $y = \frac{1}{3}x + 2$

(d)  $y = -\frac{1}{4}x + 6$

(e) None of these

$$y' = \frac{x+3-x}{(x+3)^2} = \frac{3}{(x+3)^2}$$

$$y'(6) = \frac{3}{(6+3)^2} = \frac{1}{27}$$

equation:  $y - 2 = \frac{1}{27}(x - 6)$

$$y = \frac{x}{27} + \frac{16}{9}$$

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4. [4 pts] Find the derivative of the function  $f(x) = \sqrt{3x^2 + 2e^x}$ .

$$f'(x) = \frac{1}{2}(3x^2 + 2e^x)^{-1/2} (3x^2 + 2e^x)'$$

$$= \frac{1}{2}(3x^2 + 2e^x)^{-1/2} (6x + 2e^x)$$