

Table of indefinite integrals.

1. $\int a \, dx = ax + C, a \text{ is a constant}$

2. $\int x^n dx = \frac{x^{n+1}}{n+1} + C, n \neq -1$

3. $\int \frac{dx}{x} = \ln|x| + C$

4. $\int e^x dx = e^x + C$

Properties of indefinite integrals.

For k a constant,

1. $\int kf(x)dx = k \int f(x)dx$

2. $\int (f(x) \pm g(x))dx = \int f(x)dx \pm \int g(x)dx$

Reversing the chain rule.

$$\int f'(g(x))g'(x)dx = f(g(x)) + C$$

General indefinite integral formulas.

1. $\int [f(x)]^n f'(x)dx = \frac{[f(x)]^{n+1}}{n+1} + C, \quad n \neq -1.$

2. $\int e^{f(x)} f'(x)dx = e^{f(x)} + C$

3. $\int \frac{1}{f(x)} f'(x)dx = \ln|f(x)| + C.$

Properties of the definite integral

1. $\int_a^a f(x)dx = 0$

2. $\int_a^b f(x)dx = - \int_b^a f(x)dx$

3. $\int_a^b cdx = c(b-a), \text{ where } c \text{ is a constant}$

4. $\int_a^b cf(x)dx = c \int_a^b f(x)dx, \text{ where } c \text{ is a constant}$

5. $\int_a^b [f(x) \pm g(x)]dx = \int_a^b f(x)dx \pm \int_a^b g(x)dx$

6. $\int_a^b f(x)dx = \int_a^c f(x)dx + \int_c^b f(x)dx, \text{ where } a < c < b$