$$(\ln x)' = \frac{1}{x}$$
$$(\ln(g(x))' = \frac{g'(x)}{g(x)}$$

Example 1. Differentiate each function

1. $f(x) = \sin x \ln x$

2.
$$f(x) = \ln(x^2 + 3x - 1)$$

3.
$$f(x) = \frac{1 - \ln x}{1 + \ln x}$$

$$4. \ f(x) = \ln|x|$$

Example 2. Find the equation to the tangent line to the curve $x = \ln t$, $y = te^t$ at the point (0,e).

Example 3. Find y' if $y = \ln(x^2 + y^2)$

$$(\log_a x)' = \frac{1}{x \ln a}$$
 Example 4. Find $\frac{d}{dx} (\log_3(\tan x^2))$

 $(a^x)' = a^x \ln a$ Example 5. Find $\frac{d}{dx} \left(\sqrt{2 - 3^x} + \pi^{-x} + x^e \right)$

Logarithmic differentiation

Steps in logarithmic differentiation

- 1. Take the logarithm of both sides of an equation.
- 2. Differentiate implicitly with respect to x.
- 3. Solve the resulting equation for y'.

Example 6. Differentiate each function

1. $y = x^x$

2. $y = x^{\sin x}$

3. $y = \cos(x^{\sqrt{x}})$

4.
$$y = \frac{(x+1)^4 \sqrt[5]{x^2+1}}{(x^3-1)^{10}(1+3x^2)^{2011}}$$

$$\lim_{x \to 0} (1+x)^{1/x} = e^{-\frac{1}{x}}$$