

1. Given vectors $\vec{a} = \vec{i} - 2\vec{j}$, $\vec{b} = \langle -2, 3 \rangle$. Find
 - (a) a unit vector \vec{u} that has the same direction as $2\vec{b} + \vec{a}$.
 - (b) angle between \vec{a} and \vec{b}
 - (c) $\text{comp}_{\vec{b}}\vec{a}$, $\text{proj}_{\vec{b}}\vec{a}$.
2. Find the work done by a force of 20 lb acting in the direction N50°W in moving an object 4 ft due west.
3. Find the distance from the point (-2,3) to the line $3x - 4y + 5 = 0$.
4. Find vector and parametric equations for the line passing through the points $A(1, -3)$ and $B(2, 1)$.
5. Find all points of discontinuity for the function

$$f(x) = \begin{cases} x^2 + 1 & , \text{ if } x < 2, \\ x + 2 & , \text{ if } x \geq 2. \end{cases}$$

6. Find the vertical and horizontal asymptotes of the curve $y = \frac{x^2 + 4}{3x^2 - 3}$.
7. Find $\frac{dy}{dx}$ for each function
 - (a) $y = (\sin x)^x$.
 - (b) $y = \frac{\sqrt[5]{2x-1}(x^2-4)^2}{\sqrt[3]{1+3x}}$
 - (c) $y(t) = \sin^{-1} t$, $x(t) = \cos^{-1}(t^2)$.
 - (d) $2x^2 + 2xy + y^2 = x$.
8. Find the equation of the tangent line to the curve $y = x\sqrt{5-x}$ at the point (1,2).
9. A particle moves on a vertical line so that its coordinate at time t is $y = t^3 - 12t + 3$, $t \geq 0$.
 - (a) Find the velocity and acceleration functions.
 - (b) When is the particle moving upward?
 - (c) Find the distance that particle travels in the time interval $0 \leq t \leq 3$
10. The vector function $\vec{r}(t) = \langle t, 25t - 5t^2 \rangle$ represents the position of a particle at time t . Find the velocity, speed, and acceleration at $t = 1$.
11. Find y'' if $y = e^{-5x} \cos 3x$
12. Find $\frac{d^{50}}{dx^{50}} \cos 2x$

13. A ladder 10 ft long rests against a vertical wall. If the bottom of the ladder slides away from the wall at a rate of 0.9 ft/s, how fast is the angle between the ladder and the ground changing when the bottom of the ladder is 8 ft from the wall?
14. Find the quadratic approximation of $1/x$ for x near 4.
15. If $f(x) = x + x^2 + e^x$ and $g(x) = f^{-1}(x)$, find $g'(1)$.
16. Solve the equation $\ln(x + 6) + \ln(x - 3) = \ln 5 + \ln 2$
17. Find $\cos^{-1}\left(\sin \frac{5\pi}{4}\right)$.
18. Evaluate each limit:
- $\lim_{x \rightarrow 0} \frac{\sin x + \sin 2x}{\sin 3x}$
 - $\lim_{x \rightarrow 0} (\cot x - \csc x)$
 - $\lim_{x \rightarrow 0} x^{\sin x}$
19. Find the absolute maximum and absolute minimum values of $f(x) = x^3 - 2x^2 + x$ on $[-1, 1]$.
20. For the function $y = x^2 e^x$ find
- All asymptotes.
 - Intervals on which the function is increasing/decreasing.
 - All local minima/local maxima.
 - Intervals on which the function is CU/CD.
 - Inflection points.
21. A cylindrical can without a top is made to contain V cm³ of liquid. Find the dimensions that will minimize the cost of the metal to make the can.
22. Find the derivative of the function $f(x) = \int_0^{\sqrt{x}} \frac{t^2}{t^2 + 1} dt$
23. Evaluate the integral:
- $\int_1^2 \left(x + \frac{1}{x}\right)^2 dx$
 - $\int_1^2 \frac{x^2 + 1}{\sqrt{x}} dx$
 - $\int_0^{\pi/2} (\cos t + 2 \sin t) dt$
24. Find the area under the curve $y = \sqrt{x}$ above the x -axis between 0 and 4.

25. A particle moves in a straight line and has acceleration given by $a(t) = t^2 - t$. Its initial velocity is $v(0) = 2$ cm/s and its initial displacement is $s(0) = 1$ cm. Find the position function $s(t)$.
26. Find the vector function $\vec{r}(t)$ that gives the position of a particle at time t having the acceleration $\vec{a}(t) = 2t\vec{i} + \vec{j}$, initial velocity $\vec{v}(0) = \vec{i} - \vec{j}$, and initial position $(1, 0)$.