

Chapter 8. Techniques of integration  
Section 8.1 Integration by parts

The formula for integration by parts for indefinite integrals is

$$\int f(x)g'(x)dx = f(x)g(x) - \int f'(x)g(x)dx$$

The formula for integration by parts for definite integrals is

$$\int_a^b f(x)g'(x)dx = f(x)g(x)]_a^b - \int_a^b f'(x)g(x)dx$$

**Example 1.** Find the integral.

1.  $\int \ln x \, dx$

2.  $\int \arcsin x \, dx$

3.  $\int x \cos(3x) \, dx$

4.  $\int_0^1 t^2 e^t \, dt$

5.  $\int \cos(\ln x) dx$

6.  $\int e^x \cos x dx$

**Example 2.**

1. Prove the reduction formula

$$\int \cos^n x dx = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x dx.$$

2. evaluate integral  $\int \cos^4 x \, dx$

**Example 3.** Use the methods of cylindrical shells to find the volume of a solid generated by rotating the region bounded by  $y = e^{-x}$ ,  $y = 0$ ,  $x = -1$ ,  $x = 0$  about  $x = 1$ .